

Unit 3 Boundary Representation

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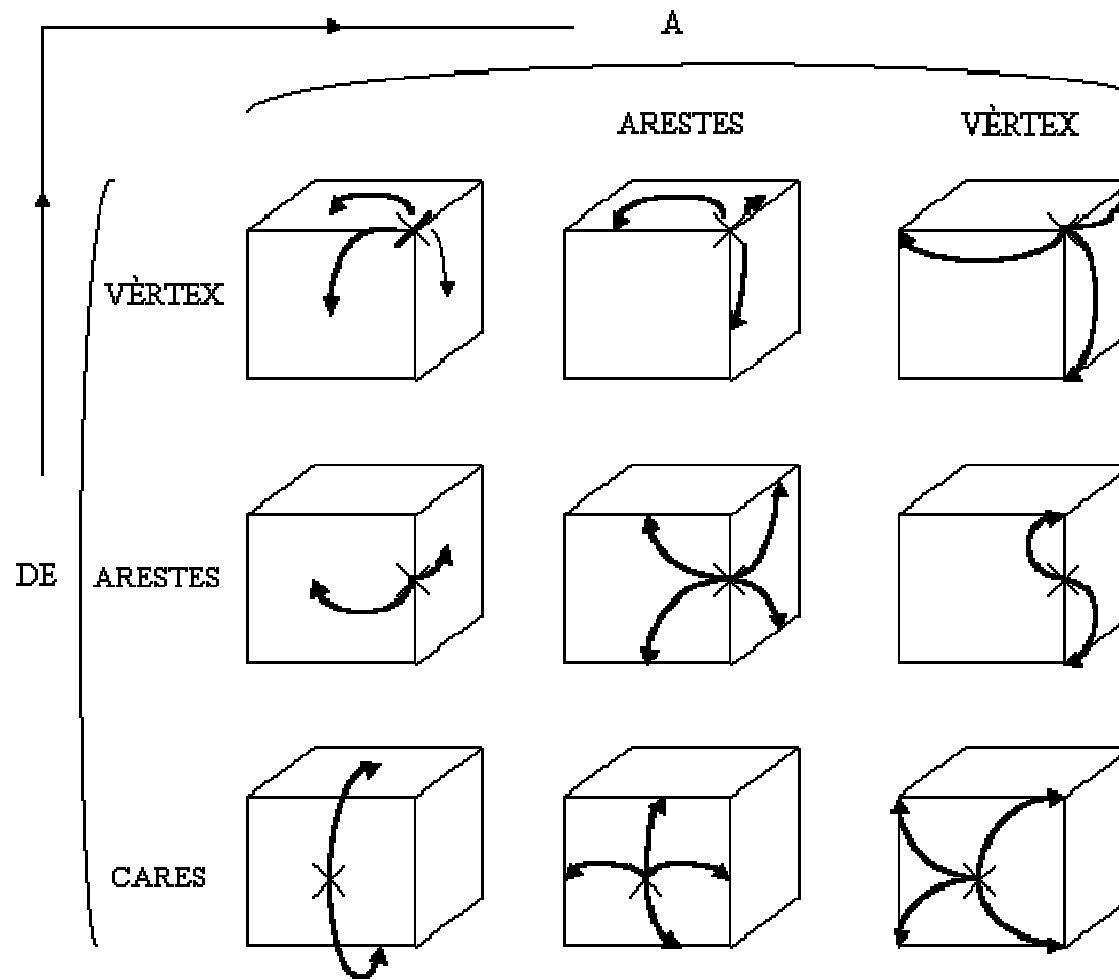
Feb 2014



Topological information

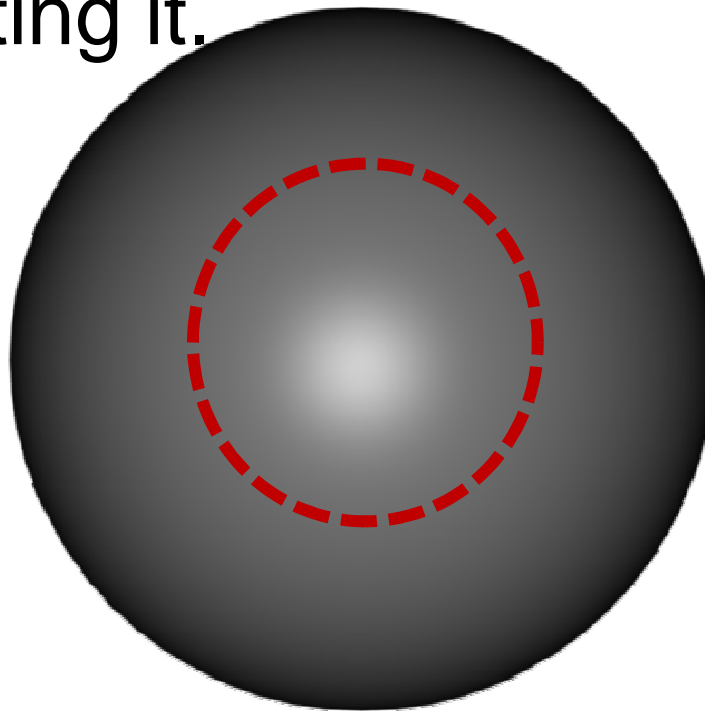
From \ To	Face	Edge	Vertex
Face	F: {F} 1:N	F: {E} 1:N	F: {V} 1:N
Edge	E: {F} 1:2	E: {E} 1:N	E: {V} 1:2
Vertex	V: {F} 1:N	V: {E} 1:N	V: {V} 1:N

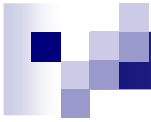
Topological information



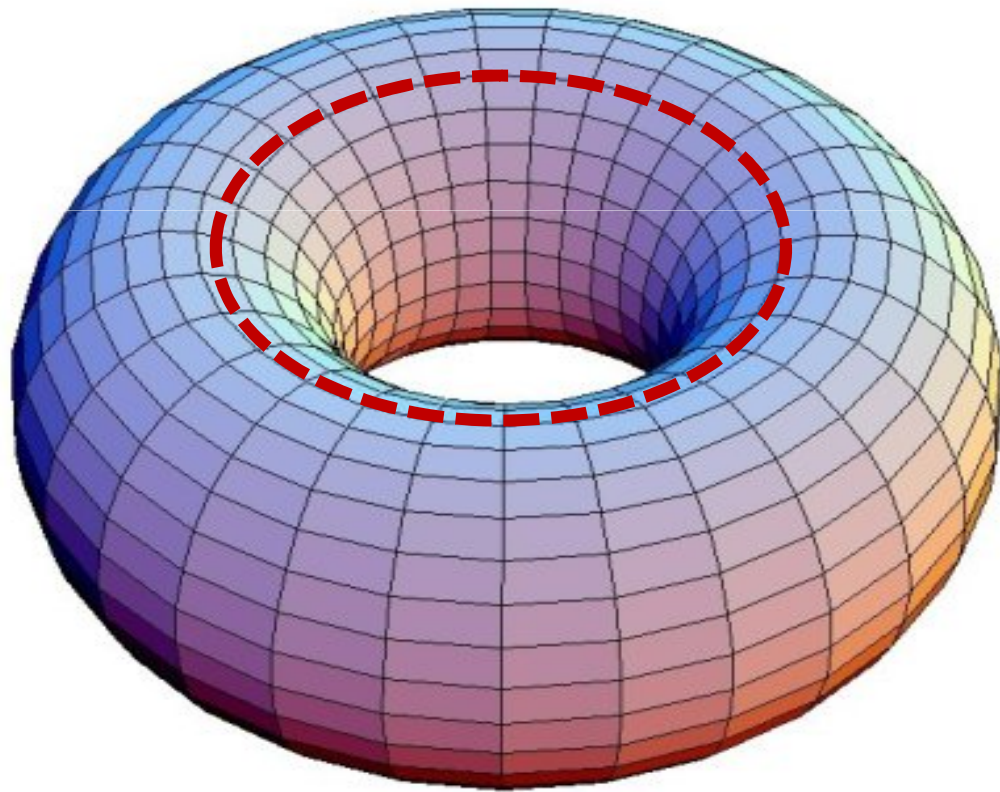
Genus (H, handles)

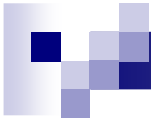
- Genus (of a surface) = maximum number of cuts (simple, closed, disjoint curves) that can be drawn on the surface without disconnecting it.



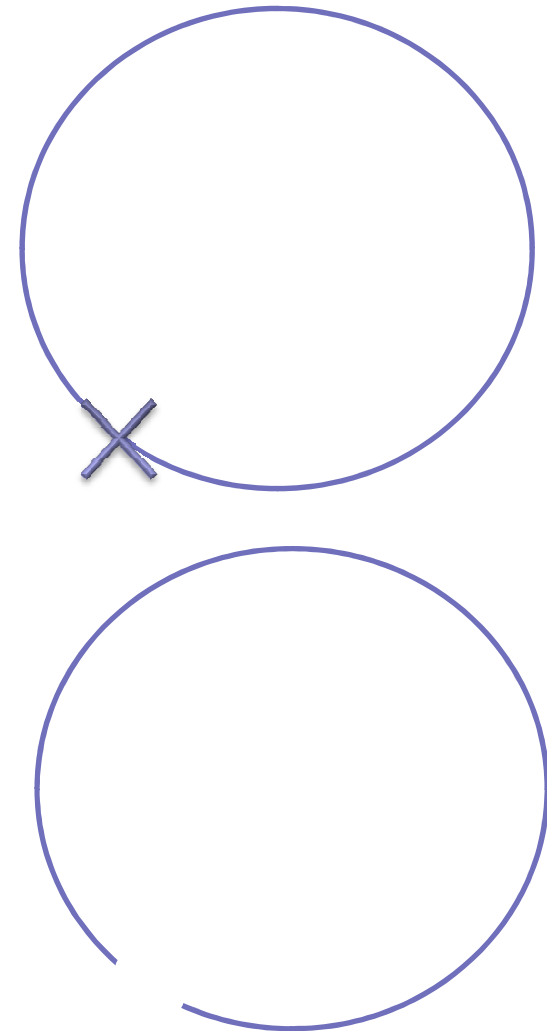
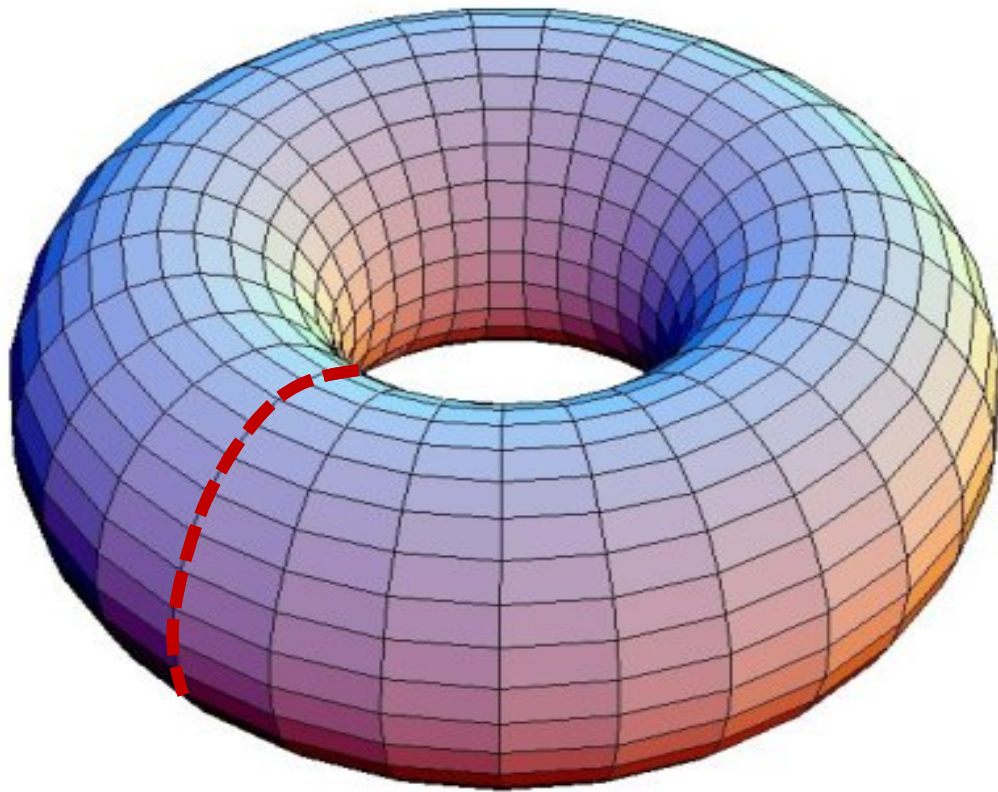


Genus 1



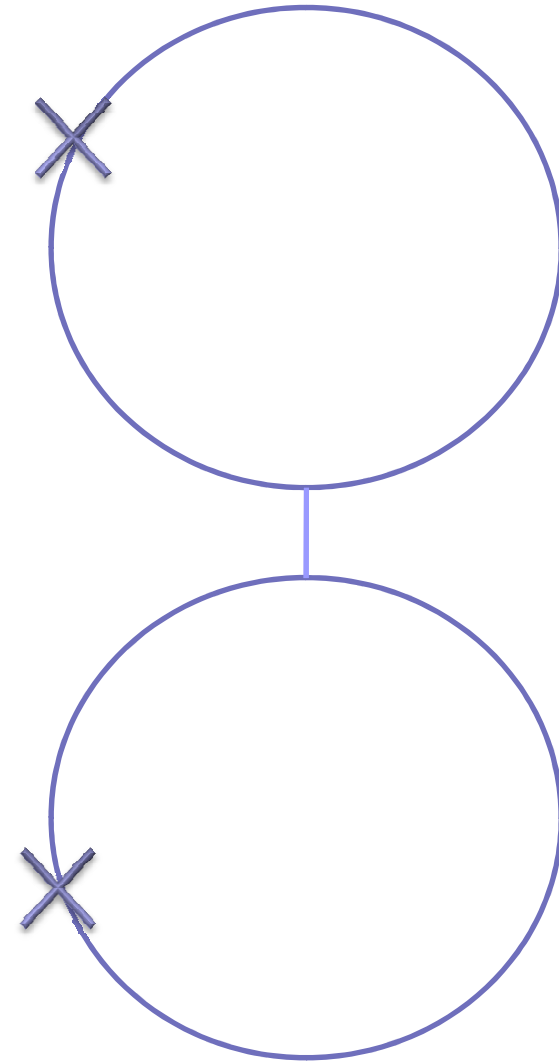
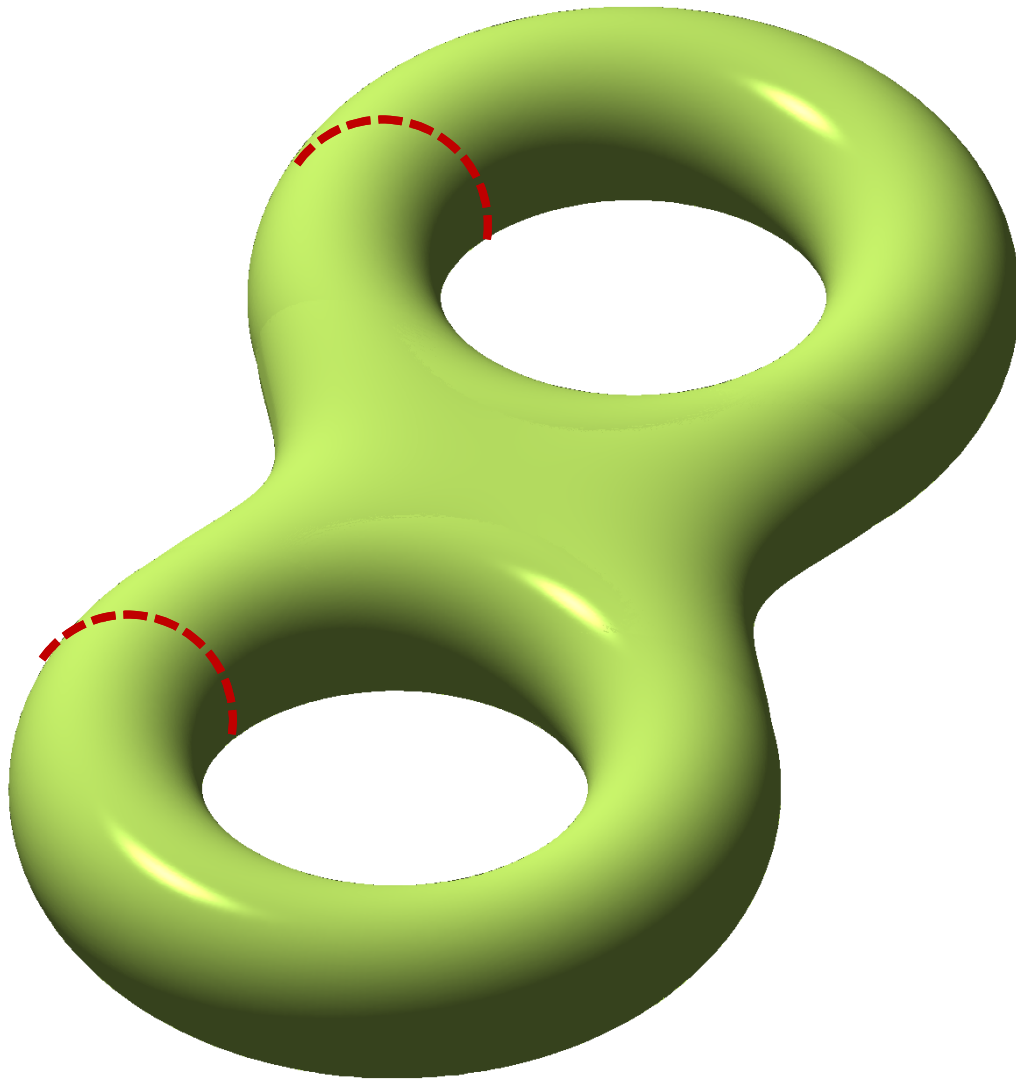


Genus 1



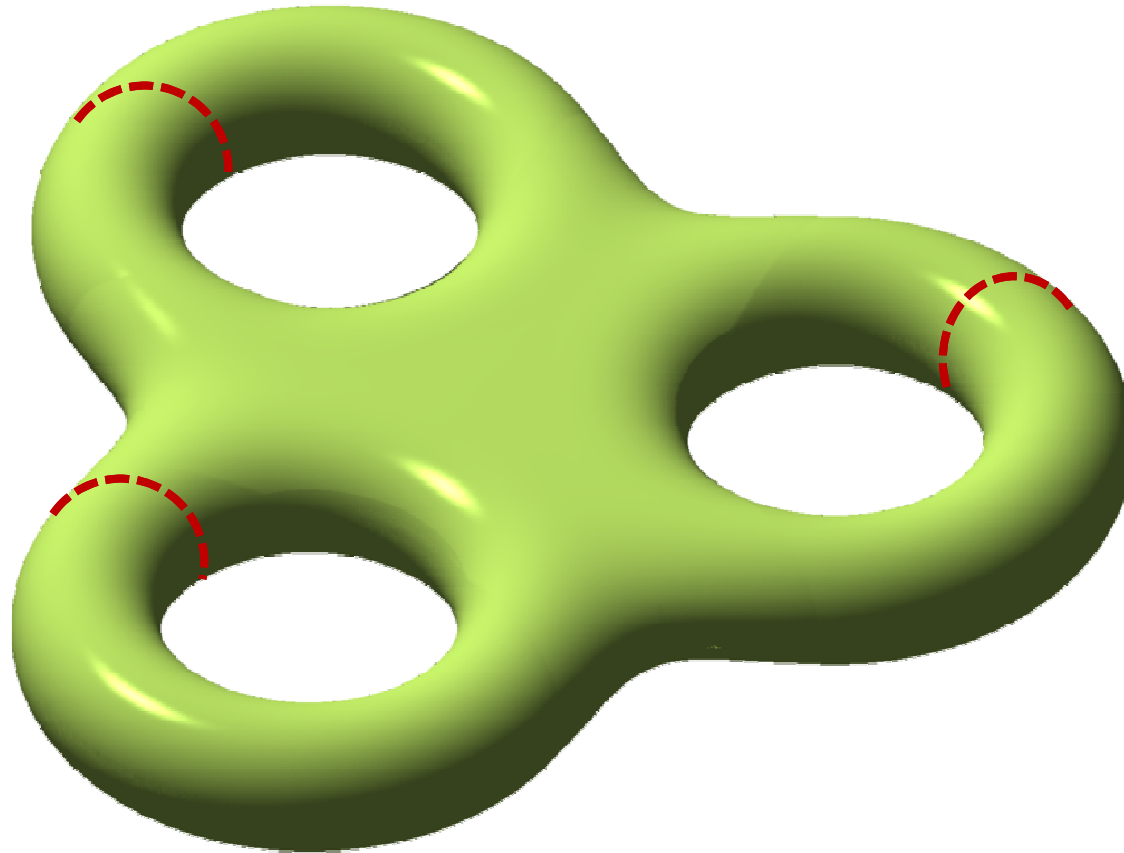


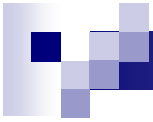
Genus 2



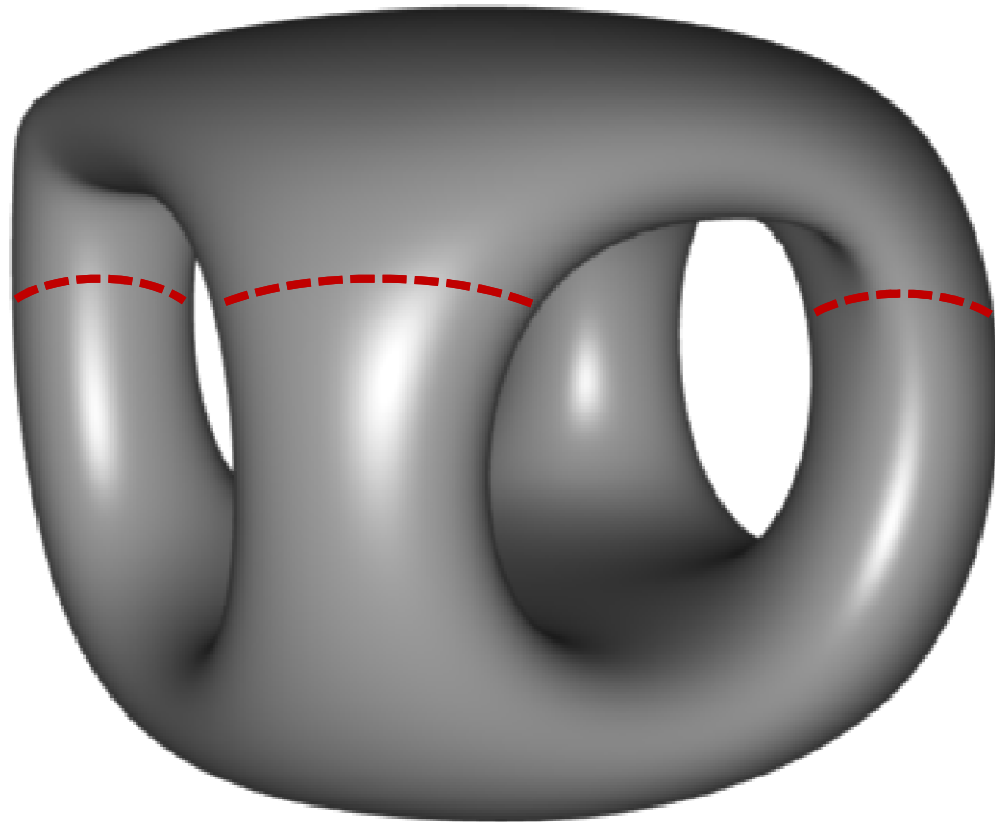


Genus 3



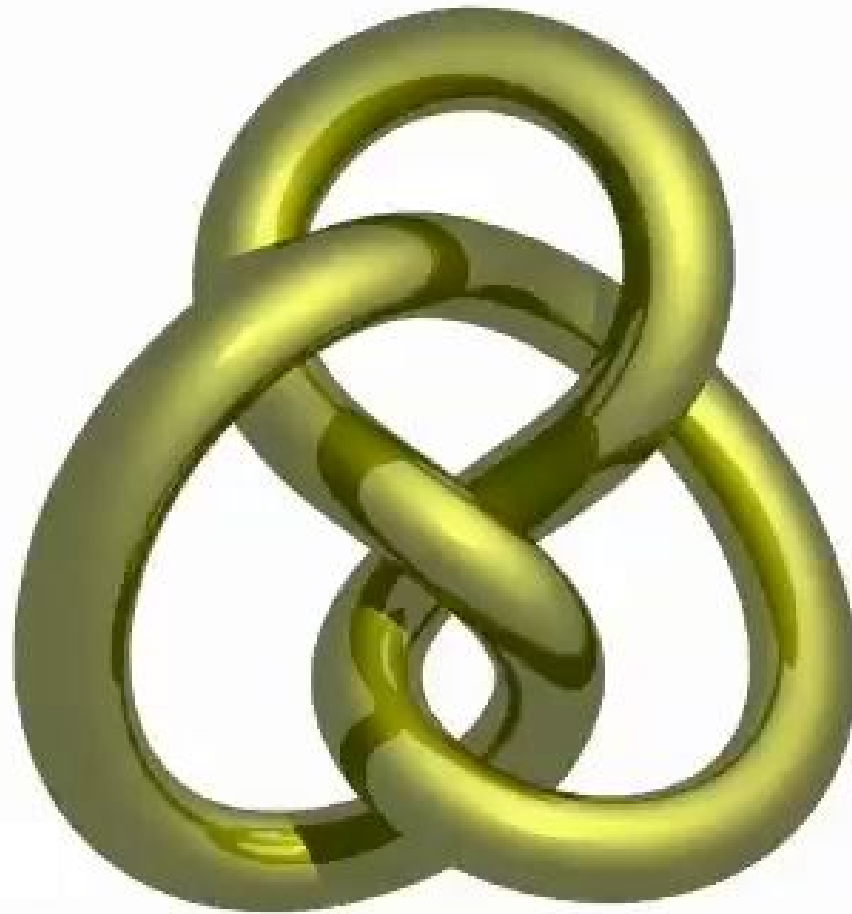


Genus 3



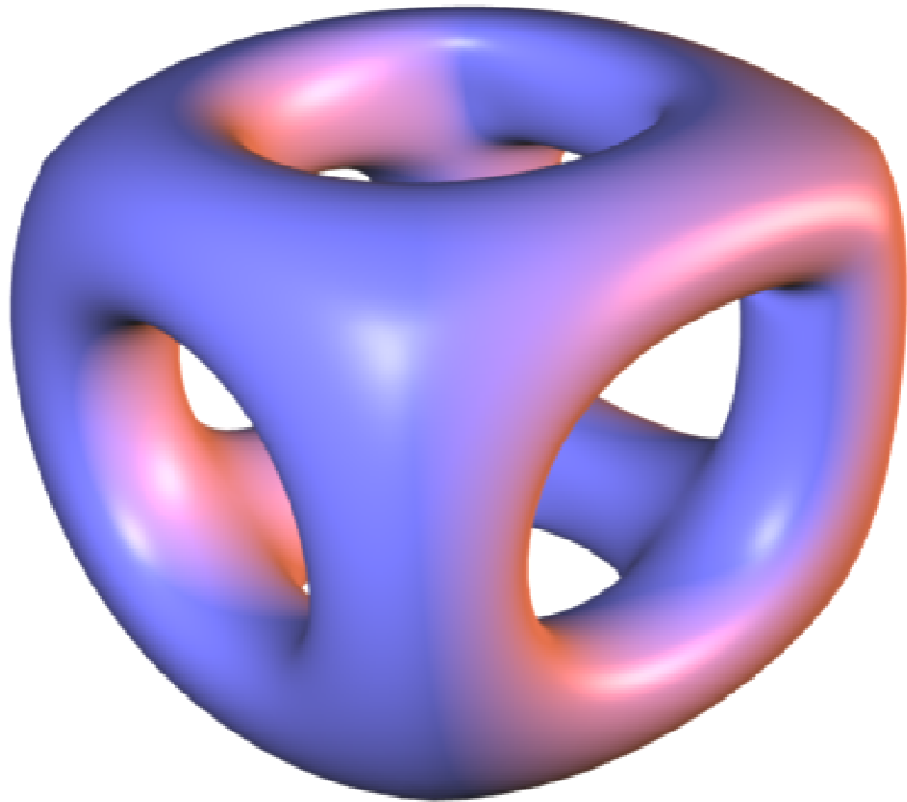


Genus?





Genus?



Euler equation for polyhedra

$$F=10 \text{ (6+4)}$$

$$V=16 \text{ (8+8)}$$

$$E=24 \text{ (12+12)}$$

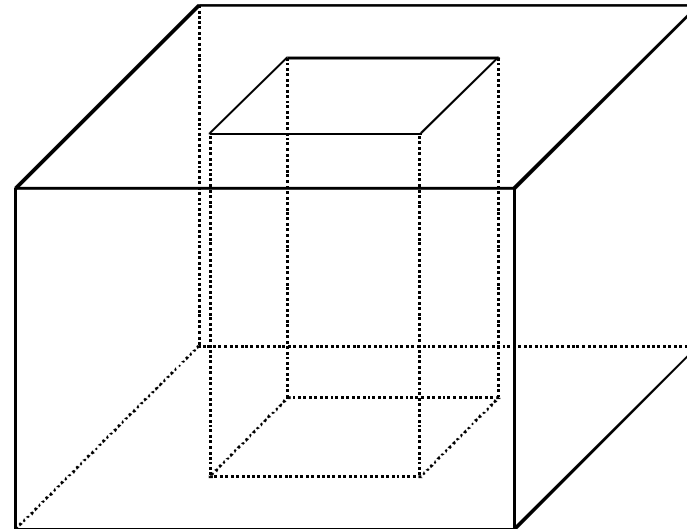
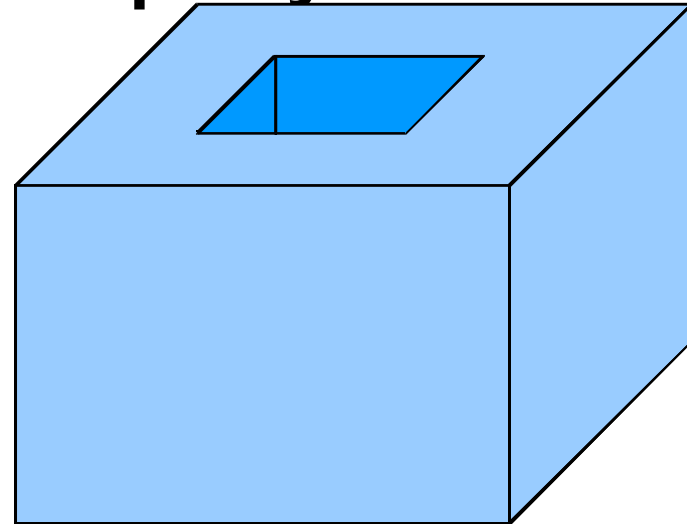
$$R=2 \text{ (two faces with a hole)}$$

$$S=1 \text{ (a single shell)}$$

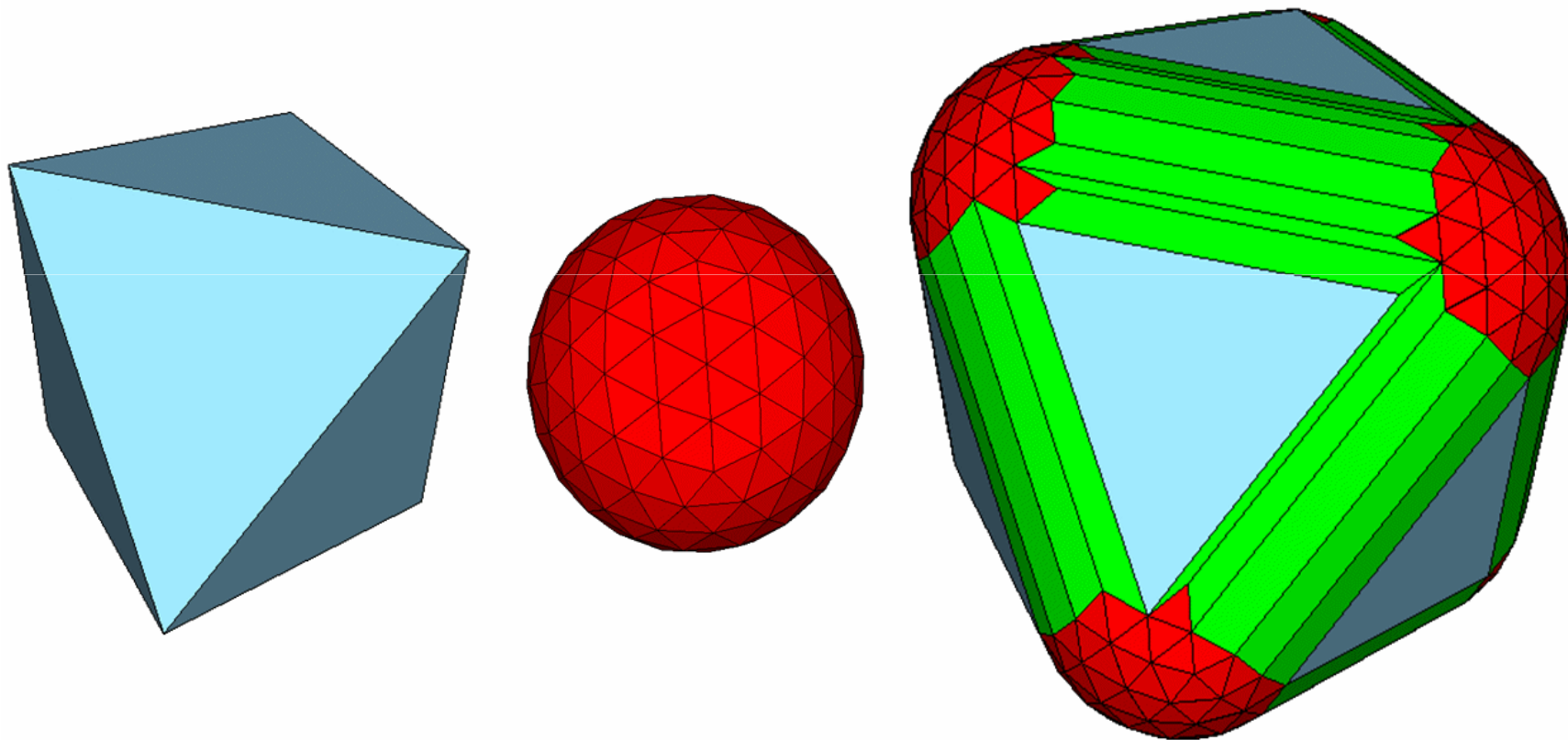
$$H=1 \text{ (a pass-through hole)}$$

$$F+V=E+R+2(S-H)$$

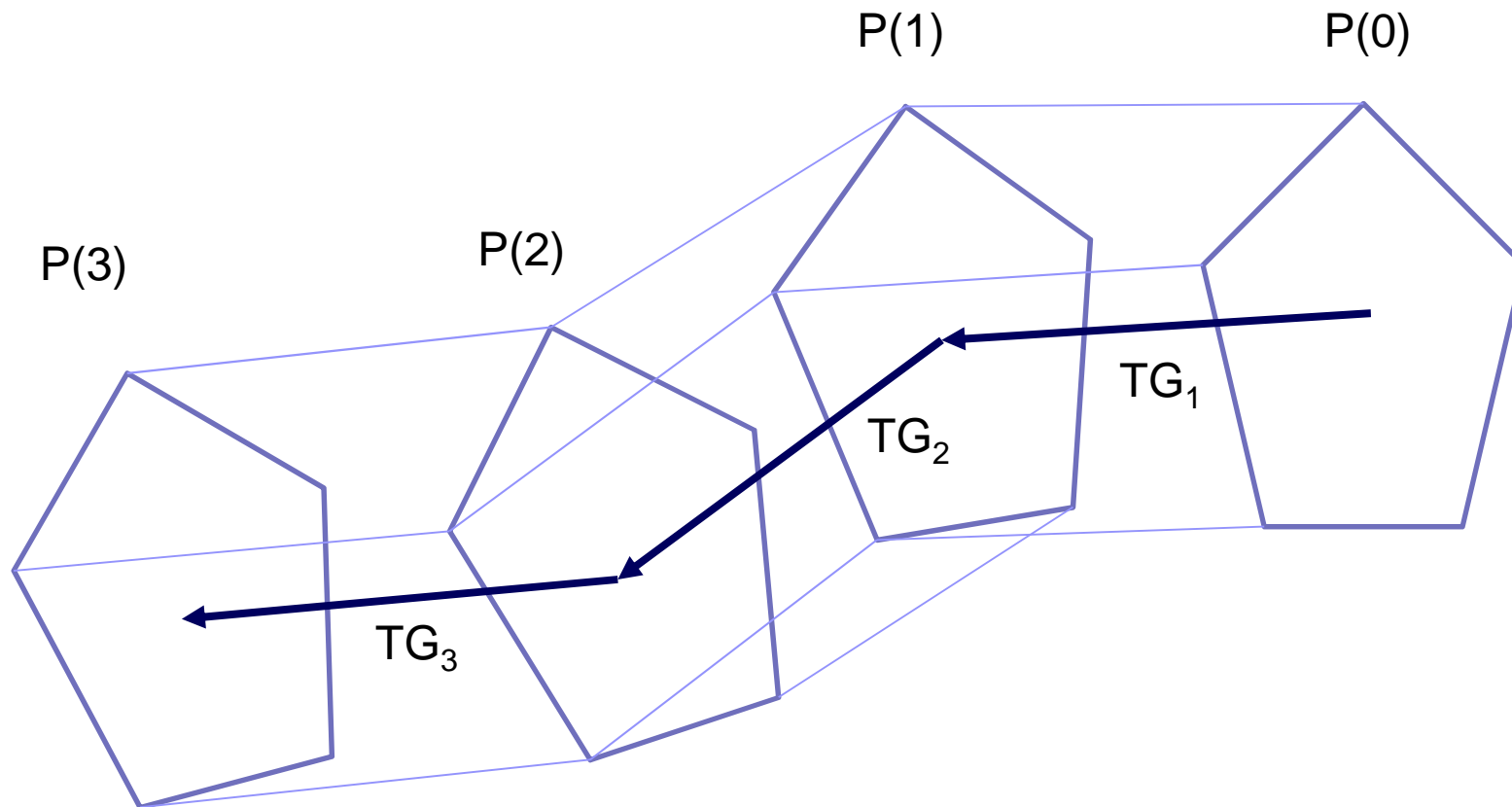
$$10+16=24+2+2*(1-1)$$



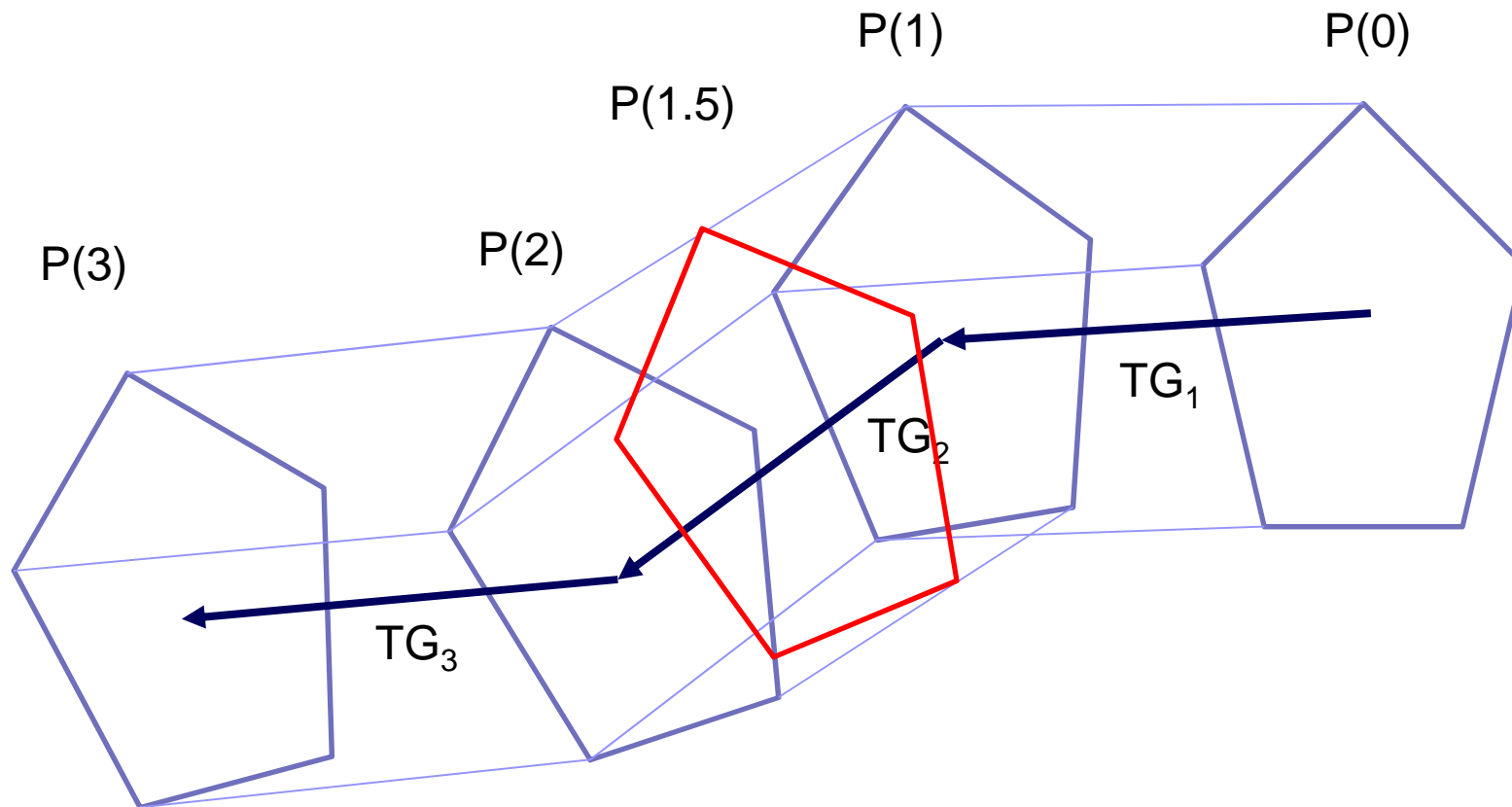
Minkoski sum



Sweep

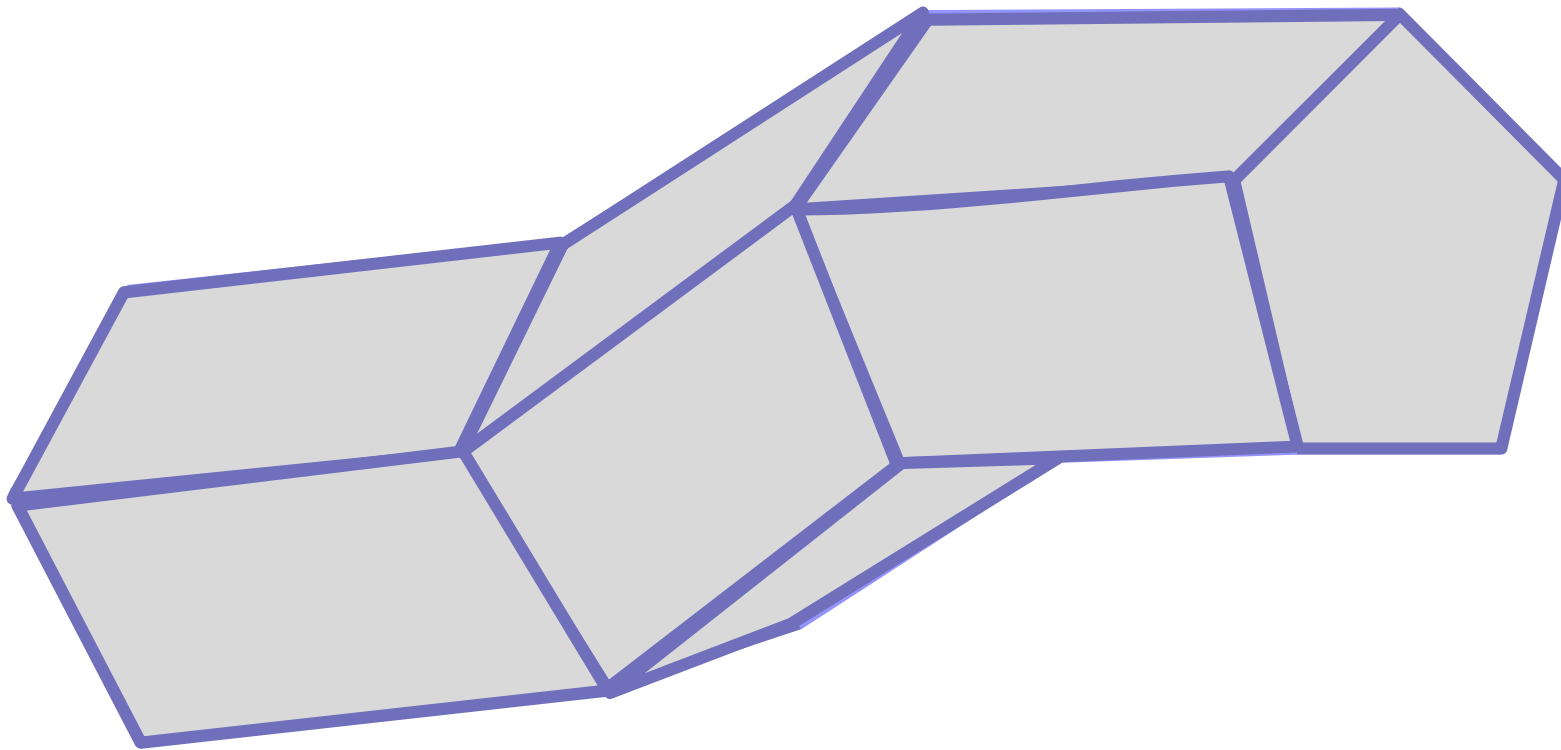


Sweep

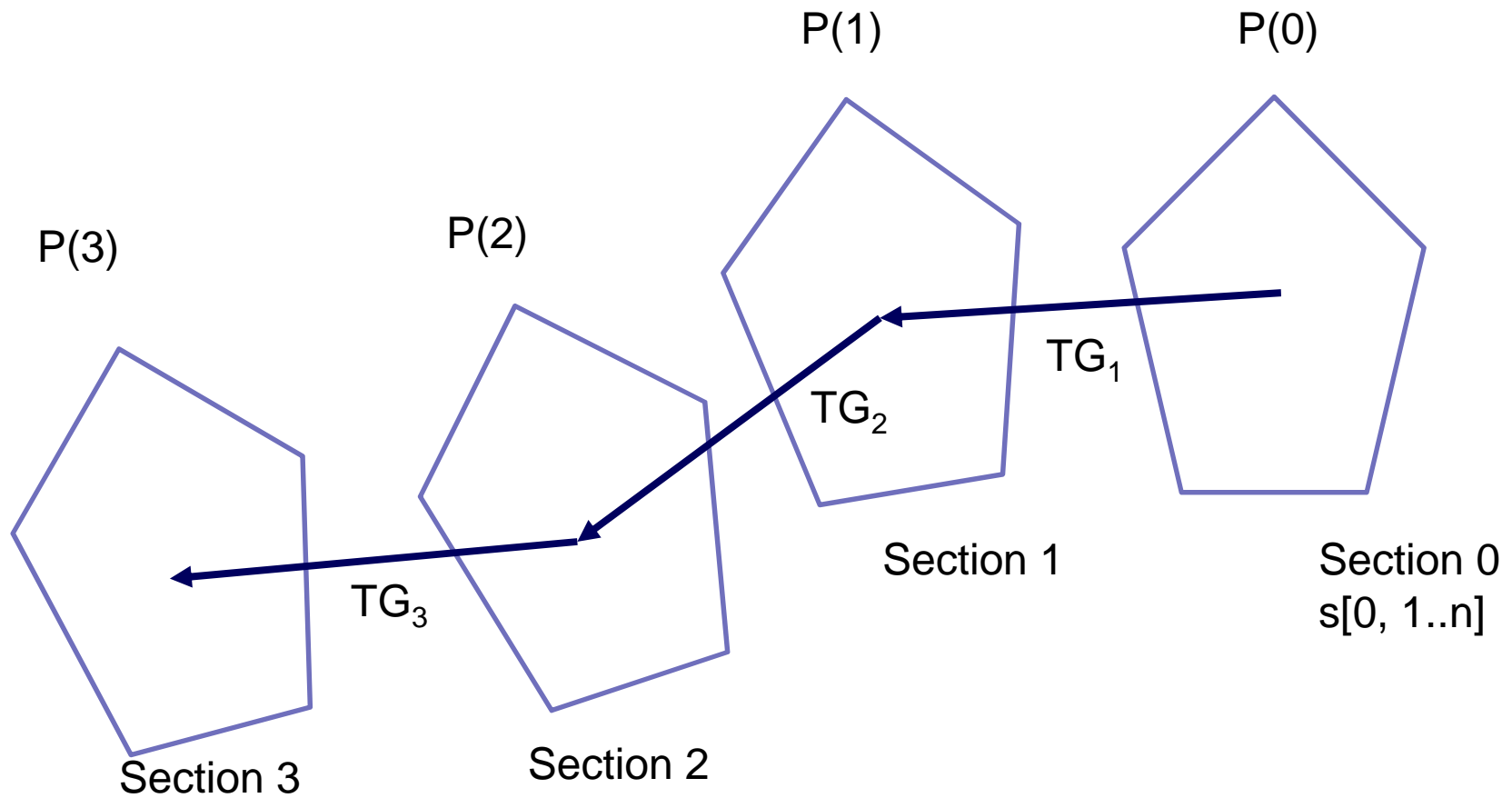




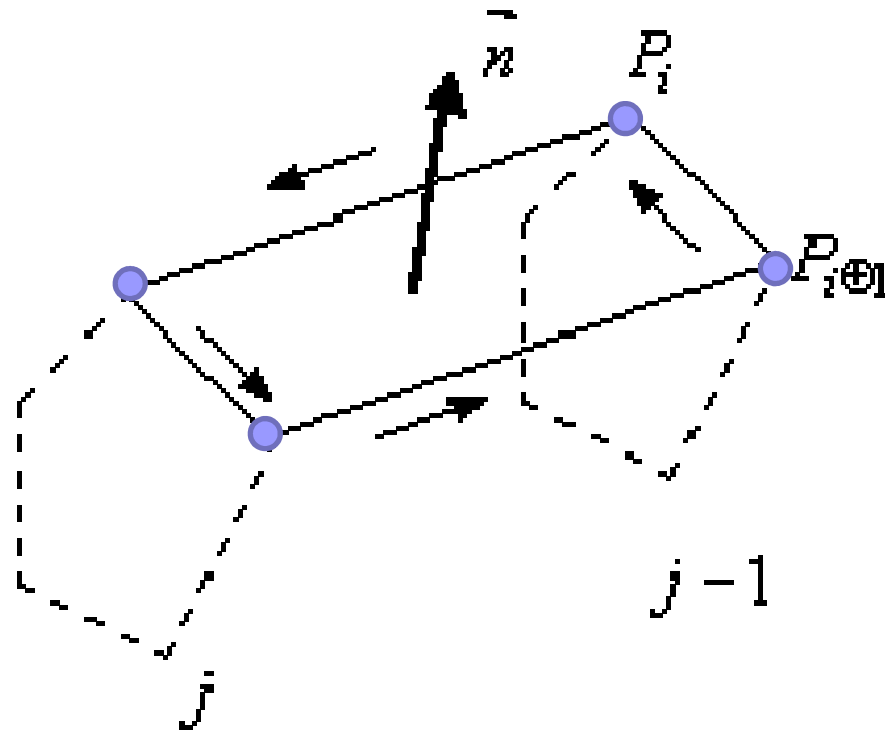
Sweep



Sweep

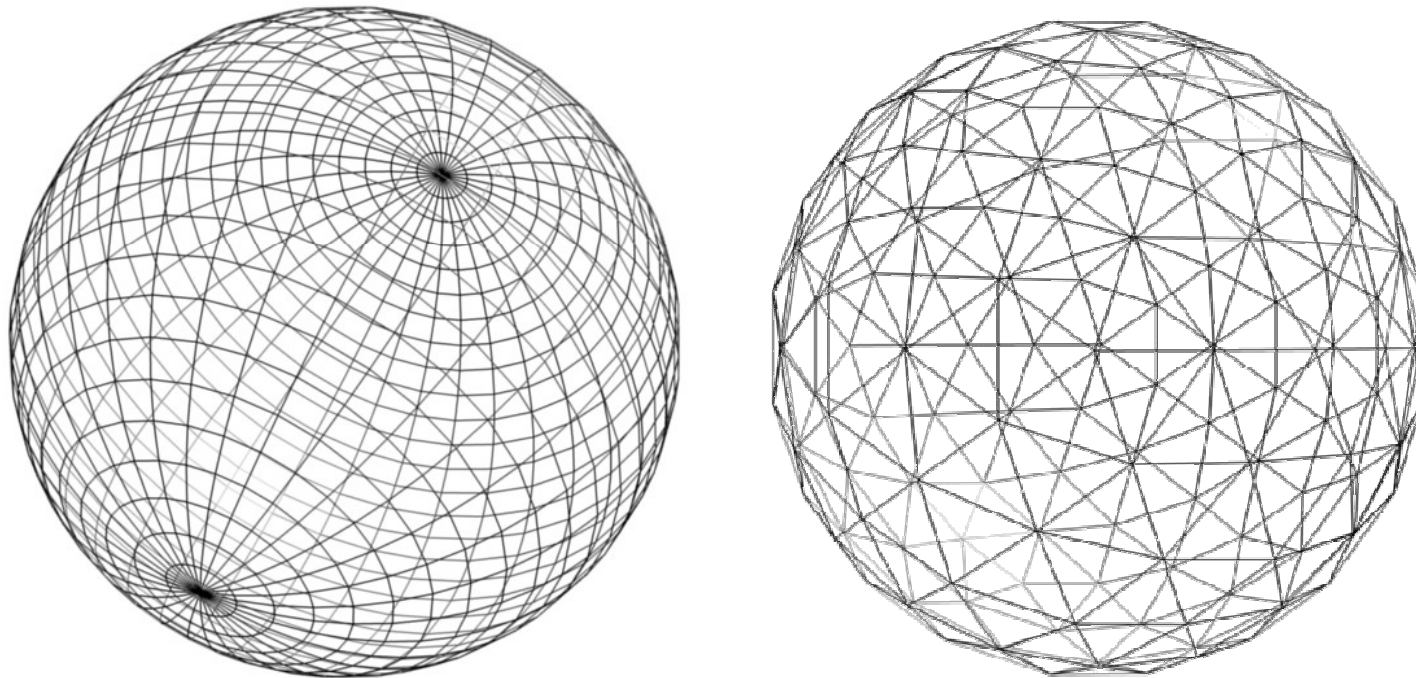


Lateral faces





Sphere approximation



Sphere approximation

