

Master in Artificial Intelligence

Morphology

Morphological
analysis

Spell checkers
and spell
correctors

Introduction to Human Language Technologies 3 - Morphology



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Outline

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Spell checkers
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- 1 Morphology
 - Motivation
 - Definitions
 - Types of morphology
- 2 Morphological analysis
 - Finite-state automata
 - Finite-state transducers
- 3 Spell checkers and spell correctors

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Motivation

There are lots of NLP tools and applications in which dealing with the morphology of the words is relevant, for instance:

- IR is based on the canonical forms of the words.
 - 'Normally, **houses** in the **Pyrenees** are made of stone.'
 - 'A typical **pyrenean house** has little windows.'
- Spell checkers are based on checking whether words in a document are well-formed or not.
 - 'This could be an **alterantive** remedy'
- Syntactic parsing requires lexical information derived from morphological analysis
 - '**Children are** very intelligent'
 - '**Children is** very intelligent'

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Definition of morphology

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- Study of the structure of words
 - Phonology: word as a combination of phonemes
 - Orthography: word as a combination of graphemes
 - Morphology: word as a combination of morphemes
- Types of morphemes:
 - Stems: (e.g., 'work', 'of', 'mak'[e])
 - Affixes: always occur combined with other morphemes (e.g., -s, 'in-', '-able')
 - Prefixes: in + frequent
 - Suffixes: work + s
 - Infixes: [Arabic] ktb + CuCuC → kutub (books)
 - Circumfixes: en+light+en
- The resulting words can be classified into categories known as Part of Speech (POS): Noun, Verb, Adjective, Adverb, Preposition, . . .

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Types of morphology

- Concatenative morphology: builds words up by concatenating morphemes (prefixes, suffixes). Frequent in the Indo-European languages.

- Inflectional morphology: *stem* → *different forms of the same word*

Ex: work → worked

Types of morphology

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- **Inflectional morphology**: *stem* → *different forms of the same word*

Ex: work → worked

- **Derivational morphology**: *stem* → *new words*

Ex: frequent → infrequent

Types of morphology

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- **Derivational morphology**: *stem* → *new words*

Ex: frequent → infrequent

- **Compositional morphology**: *N words* → *new word*

Ex: fire + man → fireman

Types of morphology

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- Concatenative morphology: builds words up by concatenating morphemes (prefixes, suffixes). Frequent in the Indo-European languages.
 - Inflectional morphology: *stem* → *different forms of the same word*
Ex: work → worked
 - Derivational morphology: *stem* → *new words*
Ex: frequent → infrequent
 - Compositional morphology: *N words* → *new word*
Ex: fire + man → fireman
- Non-concatenative morphology: builds words by other mechanism (infixes). Frequent in the Semitic languages.
 - Ex: Root-Pattern morphology
Ex: [Arabic] ktb + CaCaCa → kataba [en: he wrote]

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Goal of morphological analysis

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- Morphological recognition

Does word w belong to language L ?

- Morphological parsing

What is the morphological information related to word $w \in L$?

Ex: *word POS+Gen+Num+Case+Tense+... LEMMA (stem)*
men Noun+M+PL man

Resources required for morphological analysis

- Lists of regular (Reg) stems (ambiguities)
 - EX: Reg_V: walk
Reg_N: cat, fox, walk
- Lists of irregular (Irreg) stems (ambiguities)
 - EX: Irreg_pres_V: sing ... Irreg_past_V: sang sing
Irreg_sg_N: mouse ... Irreg_pl_N: mice
- List of suffixes and prefixes (dealing with concatenative morphology)
 - EX: Inflec: s suffix, ing suffix
Deriv: able suffix, un prefix
- Morphotactics: general rules for combining morphemes
 - EX: Reg_N + s \rightarrow PL
Reg_V + ing \rightarrow Gerund
- Spelling rules: orthographic rules for combining letters
 - EX: E-insertion: $-(z,x,s,sh,ch)^s \rightarrow -(z,x,s,sh,ch)es$
Consonant-doubling: $-l^{ing} \rightarrow -lling$

Types of morphological processors

- Based on dictionaries: list of word forms [with their corresponding morphological information]

Ex: (write VPrI write, writes VPrI3S write, wrote VPsl write, ...)

- + efficiency
- + can be automatically generated/maintained from the resources
- + language with 'simple' morphology (e.g., English)
 - languages with complex morphology (e.g., German, Finish, ...)

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Types of morphological processors

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- Based on **finite state automata (FSAs)**
 - only for lexical recognition

Types of morphological processors

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- Based on **finite state automata (FSAs)**
 - only for lexical recognition
- Based on **finite state transducers (FSTs)**
 - + useful for morphological analysis

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Finite state automata (FSA)

A FSA defines a function over words w of a regular language L .

$$M_L : w \rightarrow \{true, false\}$$

$$M = \langle Q, \Sigma, q_0, F, \sigma \rangle$$

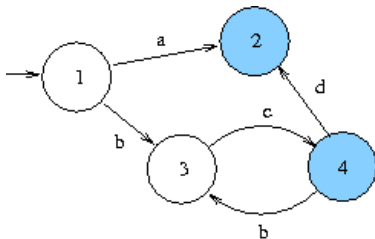
$Q = \{q_0, \dots, q_n\}$ finite set of states

$\Sigma = \{s_0, \dots, s_k\}$ finite set of symbols

$q_0 \in Q$ start state

$F \subset Q$ final states

$\sigma : Q \times \Sigma \rightarrow [Q \cup 2^Q]$ deterministic \vee non-det. transition function



$\frac{a|(bc)+d\{0,1\}}{a}$
bc
bcd
bcbcd
...

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FSAs for lexical recognition

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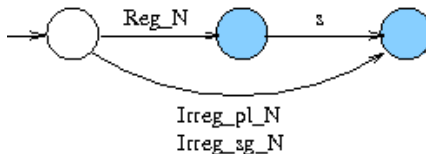
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An FSA can be the union/concatenation of different FSAs:

- FSAs generated from morphological rules
- FSAs generated from spelling rules
- FSAs generated from derivational rules
- FSAs generated from compositional rules

FSAs for lexical recognition

Example: FSA for English number nominal inflection



Examples of lists of stems

Reg_N	Irreg_sg_N	Irreg_pl_N
dog	mouse	mice
fox	foot	feet
tax		
donkey		

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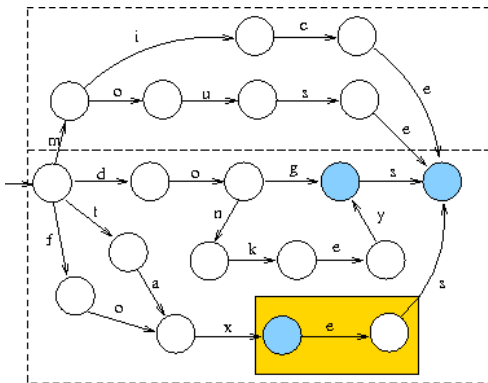
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FSAs for lexical recognition

Example: FSA for English number nominal inflection



Morphotactics: List Irreg_N

Morphotactics: noun + s = PL
over list Reg_N

SHOULD CORRECT WITH:

Spelling rule:
[s,x,z,sh,ch]^s=[s,x,z,sh,ch]es
over list Reg_N

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FSAs for lexical recognition

- FSAs can be useful for recognising words
- FSAs are not able to output a word analysis

Input word (surface form)	Output analysis (lexical form)
dog dogs (word form)	dog+N+SG dog+N+PL (lemma+Features)

- A more sophisticated technique is required: FSTs

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Finite state transducers (FSTs)

A FST defines a relation between regular languages L_1 and L_2 .

$$T = \langle Q, \Sigma, \Delta, q_0, F, \sigma, \delta \rangle$$

$Q = \{q_0, \dots, q_n\}$ finite set of states

$\Sigma = \{s_0, \dots, s_k\}$ finite set of input symbols

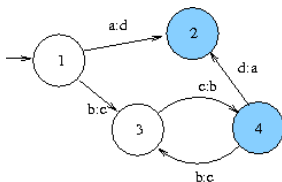
$\Delta = \{t_0, \dots, t_m\}$ finite set of output symbols

$q_0 \in Q$ start state

$F \subset Q$ final states

$\sigma : Q \times \Sigma \rightarrow 2^Q$ transition function

$\delta : Q \times \Sigma \rightarrow \Delta$ output function



$d (cb)+a\{0,1\}$	$a (bc)+d\{0,1\}$
d	a
cb	bc
cba	bcd
cbcb	bcbc
cbcb a	bcbcd
...	

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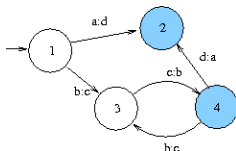
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Finite state transducers (FSTs)

- Inversion: $T : L_1 \rightarrow L_2 \implies T^{-1} : L_2 \rightarrow L_1$



$T : b:c \implies c \rightarrow b \implies \text{Ex: } cbc b \rightarrow bcb c$

$T^{-1} : b:c \implies b \rightarrow c \implies \text{Ex: } bcb c \rightarrow cbc b$

- Composition: $T_a : L_1 \rightarrow L_2 \wedge T_b : L_2 \rightarrow L_3 \implies T_a \circ T_b : L_1 \rightarrow L_3$
- $x:x \equiv x$
- Non-consumption symbol: $\epsilon \in \Sigma, \epsilon \in \Delta$

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FSTs for morphological analysis

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We want a FST being a relation between

- Surface form: $L_1 = \{w | w \text{ is word form}\}$
- Lexical form: $L_2 = \{ \langle I, F \rangle | I \text{ is lemma} \wedge F \text{ are morphological features} \}$

So that we get a morphological parser

- Ex: $\text{dogs} \rightarrow \text{dog} + \text{N} + \text{PL}$
Ex: $\text{dog} \rightarrow \text{dog} + \text{N} + \text{SG}$

Inverting that FST, we get a word forms generator

- Ex: $\text{dog} + \text{N} + \text{PL} \rightarrow \text{dogs}$
Ex: $\text{dog} + \text{N} + \text{SG} \rightarrow \text{dog}$

FSTs for morphological analysis

Two-level construction:

1 T_{lex} : A FST that computes morphotactics

Ex: $\text{Reg_N}^{\wedge} \text{s\#} \rightarrow \text{Reg_N} + \text{N} + \text{PL}$.

Ex: $\text{dog}^{\wedge} \text{s\#} \rightarrow \text{dog} + \text{N} + \text{PL}$, $\text{fox}^{\wedge} \text{s\#} \rightarrow \text{fox} + \text{N} + \text{PL}$

2 T_{inter}^i : FSTs each computing a spelling rule (orthographic regularization)

Ex: $-\{\text{z,x,s,sh,ch}\} \text{es} \rightarrow -\{\text{z,x,s,sh,ch}\}^{\wedge} \text{s\#}$

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FSTs for morphological analysis

Two-level construction:

1 T_{lex} : A FST that computes morphotactics

Ex: $\text{Reg_N}^{\wedge} \text{s\#} \rightarrow \text{Reg_N} + \text{N} + \text{PL}$.

Ex: $\text{dog}^{\wedge} \text{s\#} \rightarrow \text{dog} + \text{N} + \text{PL}$, $\text{fox}^{\wedge} \text{s\#} \rightarrow \text{fox} + \text{N} + \text{PL}$

2 T_{inter}^i : FSTs each computing a spelling rule (orthographic regularization)

Ex: $-\{z,x,s,sh,ch\}es \rightarrow -\{z,x,s,sh,ch\}^{\wedge} \text{s\#}$

Two-level processing:

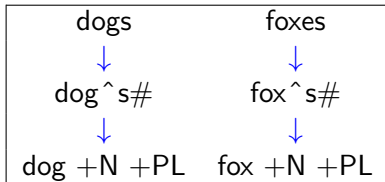
surface level

$T_{inter}^1, \dots, T_{inter}^k$

intermediate level

T_{lex}

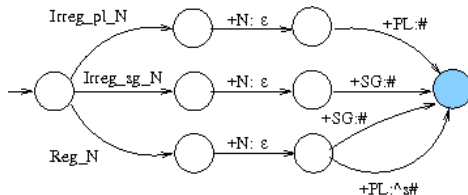
lexical level



FSTs for morphological analysis

- 1 T_{lex} : FST that computes morphotactics
Example: FST for English number nominal inflection

T_{num_nouns}



Examples of lists of stems/forms

Reg_N	Irreg_sg_N	Irreg_pl_N
dog	mouse	m o: i u: ε s: c e
fox	foot	f o: e o: e t
tax		
donkey		

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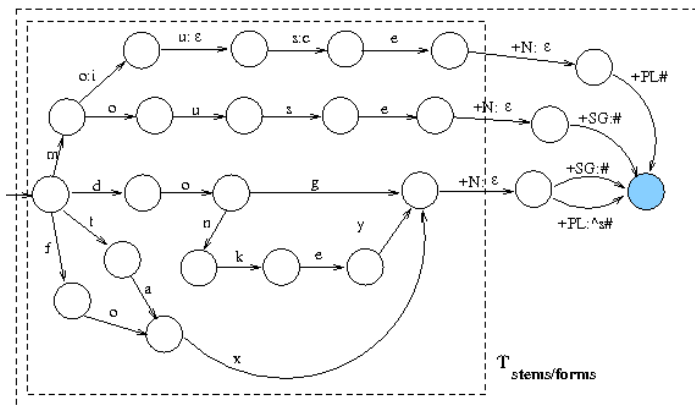
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FSTs for morphological analysis

1 T_{lex} : FST that computes morphotactics

Example: FST for English number nominal inflection

$$T_{lex} = T_{stems/forms} \circ T_{num_nouns}$$



$fox\wedge s\# \rightarrow fox+N+PL$!! (requires spelling rules)

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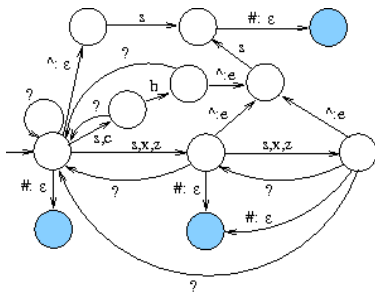
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FSTs for morphological analysis

2 T_{inter}^i : FSTs that compute spelling rules

Example: FST for E-insertion rule



'?': other symbol

e-insertion cases

foxes \rightarrow fox \wedge s $\#$

bosses \rightarrow boss \wedge s $\#$

flashes \rightarrow flash \wedge s $\#$

...

regular cases

dogs \rightarrow dog \wedge s $\#$

...

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FSTs for morphological analysis

2 T_{inter}^i : FST that computes spelling rules

Some other examples of spelling rules:

- **Consonant doubling**: two-syllable word stressed in the last one with ending CVC pattern double last consonant before *-ing/-ed*
EX: control → controlling
- **E-deletion**: Silent *-e* removed before *-ing/-ed*
EX: remove → removed
- **E-insertion**: *-e* added after ending *-s,-z,-x,-ch,-sh*, before *-s*
EX: flash → flashes
- **Y-replacement**: *-y* changes to *-ie* before *-s* or to *-i* before *-ed*
EX: cry → cries, cried
- **K-insertion**: verbs ending with *1-vowel+c* add *-k* before *-ed*
EX: panic → panicked

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Exercise

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- Generate a FST for the inflection of verbs *sing* and *work*
- Add the inflection of verb *make* to the previous FST

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Spell checkers

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- **Goal:** given a piece of text, recognise the word forms that do not belong to the text language L

- **Possible approach:**

FSA_L OR FST_L

$S = \text{Tokenizer}(\text{text})$ (sequence of forms)

for each $x \in S$

if $FSA_L(x)$ then print("x")

else print("**x**")

Spell correctors

- **Goal:** given a word form, provide a list of possible correct forms.

- **Possible approach:**

$D = \{y_i : y_i \in L\}$ generated by applying FST_L

$S = \text{Tokenizer}(\text{text})$ (sequence of forms)

for each $x \in S$

if $x \in D$ then print(x)

else

$D' = \{y \in D : |\text{length}(x) - \text{length}(y)| \leq \gamma\}$

$C = \emptyset$

for each $y \in D'$

$d = \text{distance}(x, y)$

if $(d \leq \delta)$ then

$C = C + \{< y, d >\}$

print_Nbest_candidates(C, N)

$\delta = 2$ and $\gamma = 2$ seem to be enough for standard text

Spell correctors

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- Edit distance: minimum number of insertions, deletions, swaps to achieve y from x
- **Weighted edit distance**: minimum **cost** of insertions, deletions, swaps to achieve y from x
 - Cost of insertion/deletion = 1
 - Cost of swap = $s(a, b)$: (typo - Manhattan distance in a keyboard)
 - Total cost = $d(x, y)$:
 - Compute cost matrix E , with dimension $m \times n$ (lengths of x and y) using dynamic programming
 - $d(x, y) = E(m, n)$

Spell correctors

Cost matrix computation

	y1	y2	y3	y4	
	0	1	2	3	4
x1	1				
x2	2				
x3	3				

deletion (+1)

insertion (+1)

swap

$+s(x_i, y_j)$

$$E(i, j) = \min(\text{Cost}_{del}, \text{Cost}_{ins}, \text{Cost}_{swap})$$

$$\begin{cases} \text{Cost}_{del} = E(i-1, j) + 1 \\ \text{Cost}_{ins} = E(i, j-1) + 1 \\ \text{Cost}_{swap} = E(i-1, j-1) + s(x_i, y_j) \end{cases}$$

$s(x_i, y_j)$	a	b	c	d	e
a	0				
b	0.5	0			
c	0.3	0.3	0		
d	0.2	0.2	0.1	0	
e	0.3	0.4	0.2	0.1	0

$s(x_i, y_j)$ normalised to 1.0

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- Compute the weighted edit distance between 'dom' and 'come'