

Advanced Human Language Technologies

Similarity Models

Similarity
Models

Edit Distances

Vector/Set
similarities
and distances

Knowledge-
based
Approaches

Corpus-based
representa-
tions



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Outline

1 Similarity Models

2 Edit Distances

3 Vector/Set similarities and distances

- Vector similarities and distances
- Set similarities and distances

4 Knowledge-based Approaches

5 Corpus-based representations

- Sparse vector representations
 - Term-Term Matrix (using PMI)
 - Term-Document Matrix (using TF-IDF)
- Dense representations
 - LSA
 - Word Embeddings

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Similarity Models

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- Similarity models measure how alike are two objects (products, patients, molecules, words, sentences, ...).
- Objects (words, sentences, documents...) are represented as feature-vectors, feature-sets, distribution-vectors, ...
- *Similarity* may also be interpreted as *proximity* or *affinity*
- *Similarity* may also be seen as the opposite of *distance*, *difference*, or *divergence*.
- Different uses and applications in AI.

Applications of Similarity Models

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- **Recommendation systems.** E.g. finding similar patients to propose similar treatments, finding similar products to offer them as potentially interesting, find similar news items to recommend, etc.
- **Prediction systems.** (Example-based Learning, EBL). E.g. predict possible diagnoses based on similar patients, predict product sales based on similar products, classify news items based on similar texts, etc.
- **Clustering systems.** E.g.: Group data in clusters to discover new patterns, offer aggregated views to the user, speed up searches, etc.

Applications of Similarity Models to HLT

- **Text similarity tasks:** Plagiarism detection, news items tracking, related readings recommendation, question answering, FAQ management, ...
- **Text analysis tasks:** Tasks such as PoS Tagging, parsing, NERC, etc can be approached using EBL.
- **Text Classification tasks:** (EBL, again). E.g.: news items routing, sentiment analysis, spam detection, ...
- **Evaluation of NL generation tasks:** Evaluate machine translation, automatic summarization, or report generation comparing the system output with reference texts.
- **Alias detection:** (Useful for coreference detection) find different mentions of the same entity (e.g. *Stanford President John Hennessy*, *Stanford University President Hennessy*, *President John Hennessy*, *Stanford Provost John Hindirck*).

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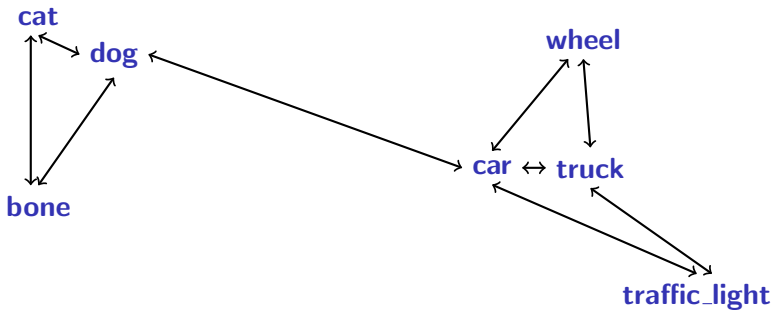
Distance, Similarity, & Relatedness

- We talk about *distance* when metric properties hold:
 - $d(x, x) = 0$
 - $d(x, y) > 0$ when $x \neq y$
 - $d(x, y) = d(y, x)$ (simmetry)
 - $d(x, z) \leq d(x, y) + d(y, z)$ (triangular inequation)
- We use *similarity* in the general case
 - Function: $\text{sim} : A \times B \rightarrow S$ (where S is often $[0, 1]$)
 - Homogeneous: $\text{sim} : A \times A \rightarrow S$ (e.g. word-to-word)
 - Heterogeneous: $\text{sim} : A \times B \rightarrow S$ (e.g. word-to-document)
 - Not necessarily symmetric, or holding triangular inequation.
- We can compute one from the other:

$$\text{sim}(A, B) = \frac{1}{1 + d(A, B)}; \quad d(A, B) = \frac{1}{\text{sim}(A, B)} - 1$$

- *Similarity* is often interpreted as a measure of *relatedness*.

Distance, Similarity, & Relatedness



$d(\text{car}, \text{wheel}) > d(\text{car}, \text{truck});$
 $d(\text{car}, \text{dog}) \gg d(\text{car}, \text{truck});$
 $d(\text{cat}, \text{bone}) > d(\text{dog}, \text{bone});$

$\text{sim}(\text{car}, \text{wheel}) < \text{sim}(\text{car}, \text{truck});$
 $\text{sim}(\text{car}, \text{dog}) \ll \text{sim}(\text{car}, \text{truck});$
 $\text{sim}(\text{cat}, \text{bone}) < \text{sim}(\text{dog}, \text{bone});$

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Information used to compute similarity

The utility/meaning of a similarity/distance measure depends on how compared objects are represented.

- Information internal to compared units

- Words: char n-grams, word form, lemma, morphology, PoS, sense, domain, ...
- Sentences/Documents: bag of words, parse tree, syntactic roles, collocations, word n-grams, Named Entities, ...

- Information external to compared units (context)

- Words: bag-of-words in context, parse tree, collocations, word n-grams, Named Entities, ...
- Sentences/Documents: Words in nearby sentences, document meta-information, ...

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Approaches to Similarity Computation

- **String/Sequence edit-distance approaches.**

Can only be applied to sequences of elements (characters, words, proteins...)

- **Vector/Set based approaches.**

General approach, can be applied to any kind of object once we represent it as a [feature] vector or set.

- Vector similarities/distances
- Set similarities/distances

- **Knowledge-based approaches.**

Require some (graph-like) knowledge representation.

- WordNet distances

- **Corpus-based approaches (distributional semantics).**

Describe meaning based on occurrence contexts.

- Sparse representations (term-term/term-document matrix)
- Dense representations (LSI, Word Embeddings)

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String/Sequence edit-distance approaches

Sequences of any kind

- word : sequence of characters
- sentence : sequence of words (or characters too)
- DNA: sequence of bases A,T,C,G
- Health Record : sequence of clinical events
- ...

Some Edit Distances

- LCS (Longest Common Subsequence): ED allowing deletion and insertion.
- Levenshtein: ED allowing deletion, insertion and substitution.
- Damerau-Levenshtein: ED allowing insertion, deletion, substitution, and transposition of two adjacent elements.

Edit distances can be efficiently computed using dynamic programming.

Example: Levenhstein

```
1 def Levenshtein(s, t):
2
3     n = len(s)
4     m = len(t)
5     d = [ [ 0 for j in range(0,m+1) ] for i in range(0,n+1) ]
6
7     # source prefixes can be transformed into empty string by
8     # dropping all characters
9     for i in range(1,n+1): d[i][0] = i
10
11    # target prefixes can be reached from empty source prefix
12    # by inserting every character
13    for j in range(1,m+1): d[0][j] = j
14
15    for i in range(1,n+1):
16        for j in range(1,m+1):
17
18            subst = 0 if s[i-1] == t[j-1] else 1 # substitution cost
19
20            d[i][j] = min(d[i-1][j] + 1,          # deletion
21                        d[i][j-1] + 1,          # insertion
22                        d[i-1][j-1] + subst)    # substitution
23
24    return d[n][m]
```

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Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ									
S									
U									
N									
D									
A									
Y									

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1								
U	2								
N	3								
D	4								
A	5								
Y	6								

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0							
U	2								
N	3								
D	4								
A	5								
Y	6								

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0	1						
U	2	1	1						
N	3								
D	4								
A	5								
Y	6								

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0	1	2					
U	2	1	1	2					
N	3	2	2	2					
D	4								
A	5								
Y	6								

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0	1	2	3				
U	2	1	1	2	2				
N	3	2	2	2	3				
D	4	3	3	3	3				
A	5								
Y	6								

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0	1	2	3	4			
U	2	1	1	2	2	3			
N	3	2	2	2	3	3			
D	4	3	3	3	3				
A	5								
Y	6								

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0	1	2	3	4	5		
U	2	1	1	2	2	3	4		
N	3	2	2	2	3	3	4		
D	4	3	3	3	3	4	3		
A	5	4	3	4	4	4			
Y	6								

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0	1	2	3	4	5	6	
U	2	1	1	2	2	3	4	5	
N	3	2	2	2	3	3	4	5	
D	4	3	3	3	3	4	3	4	
A	5	4	3	4	4	4	4	3	
Y	6	5	4	4					

Example: Levenhstein

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	λ	S	A	T	U	R	D	A	Y
λ	0	1	2	3	4	5	6	7	8
S	1	0	1	2	3	4	5	6	7
U	2	1	1	2	2	3	4	5	6
N	3	2	2	2	3	3	4	5	6
D	4	3	3	3	3	4	3	4	5
A	5	4	3	4	4	4	4	3	4
Y	6	5	4	4	5	5	5	4	3

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λ	The spokesman said the senior advisor was shot dead
λ Spokesman confirms senior government advisor was shot	

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Vector similarities/distances

When objects are represented as [feature] vectors, we can use vector-space distances.

- Manhattan distance
- Euclidean distance
- Chebychev distance
- Camberra distance
- Cosine *similarity*
- Dot Product *similarity*
- ...

Vector similarities/distances

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- Commonly used norms belong to the family of Minkowsky distances:

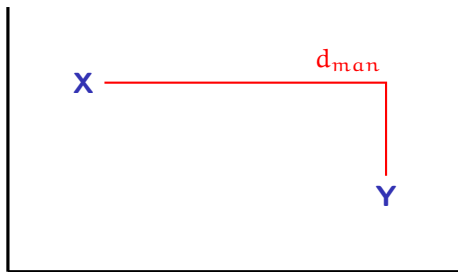
$$d_{\min}(\vec{x}, \vec{y}) = L_r(\vec{x}, \vec{y}) = \left(\sum_{i=1}^N |x_i - y_i|^r \right)^{\frac{1}{r}}$$

- L_1 and L_2 norms are particular cases of orders 1 and 2
- Chebychev distance is the limit L_∞ .

Vector similarities/distances

- L_1 norm, a.k.a. Manhattan distance, taxi-cab distance, city-block distance:

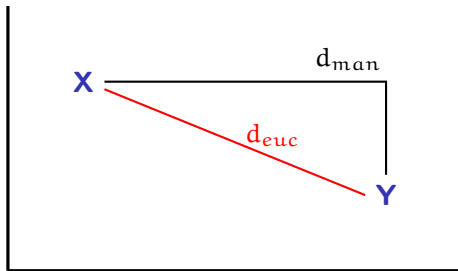
$$d_{\text{man}}(\vec{x}, \vec{y}) = L_1(\vec{x}, \vec{y}) = \sum_{i=1}^N |x_i - y_i|$$



Vector similarities/distances

- L_2 norm, a.k.a. Euclidean distance:

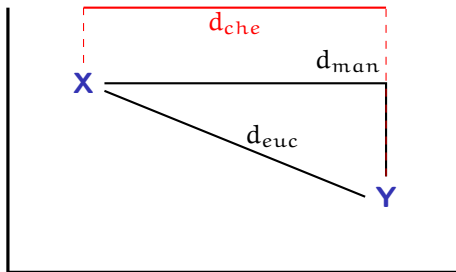
$$d_{\text{euc}}(\vec{x}, \vec{y}) = L_2(\vec{x}, \vec{y}) = |\vec{x} - \vec{y}| = \sqrt{\sum_{i=1}^N (x_i - y_i)^2}$$



Vector similarities/distances

- The limit of Minkowsky distance is Chebychev distance:

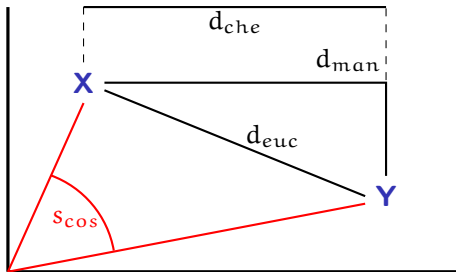
$$d_{che}(\vec{x}, \vec{y}) = L_{\infty} = \lim_{r \rightarrow \infty} L_r(\vec{x}, \vec{y}) = \max_i |x_i - y_i|$$



Vector similarities/distances

- Cosine is a similarity, not a distance:

$$\text{sim}_{\cos}(\vec{x}, \vec{y}) = \cos(\vec{x}, \vec{y}) = \frac{\vec{x} \cdot \vec{y}}{|\vec{x}| \cdot |\vec{y}|} = \frac{\sum_i x_i y_i}{\sqrt{\sum_i x_i^2} \cdot \sqrt{\sum_i y_i^2}}$$



Vector similarities/distances

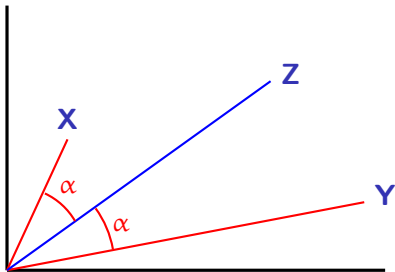
- Dot product (or scalar product) is also similarity, that takes into account not only the angle but also the norm of the vectors:

$$\text{sim}_{\text{dot}}(\vec{x}, \vec{y}) = \vec{x} \cdot \vec{y} = \sum_i x_i y_i$$

$$\begin{aligned}\text{sim}_{\cos}(X, Z) &= \text{sim}_{\cos}(Y, Z) \\ &= \cos \alpha \approx 0.84\end{aligned}$$

$$\text{sim}_{\text{dot}}(X, Z) = X \cdot Z \approx 8.2$$

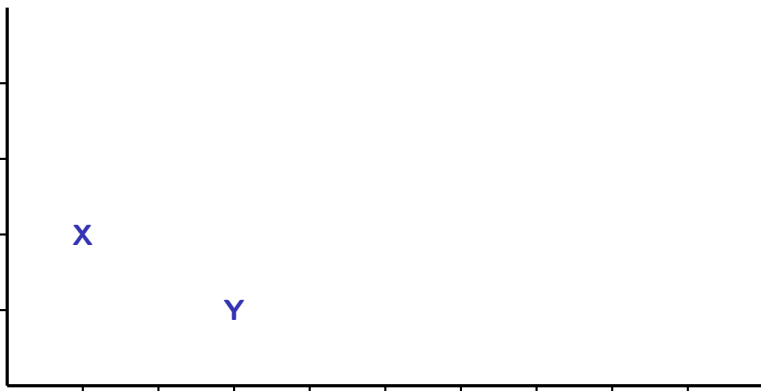
$$\text{sim}_{\text{dot}}(Y, Z) = Y \cdot Z \approx 21.3$$



Vector similarities/distances

- Canberra distance is similar to L_1 but relative to the distance to origin:

$$d_{\text{cam}}(\vec{x}, \vec{y}) = \sum_{i=1}^N \frac{|x_i - y_i|}{|x_i| + |y_i|}$$



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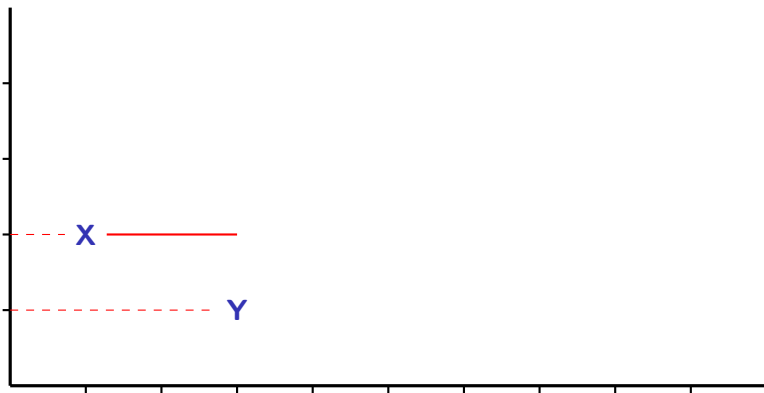
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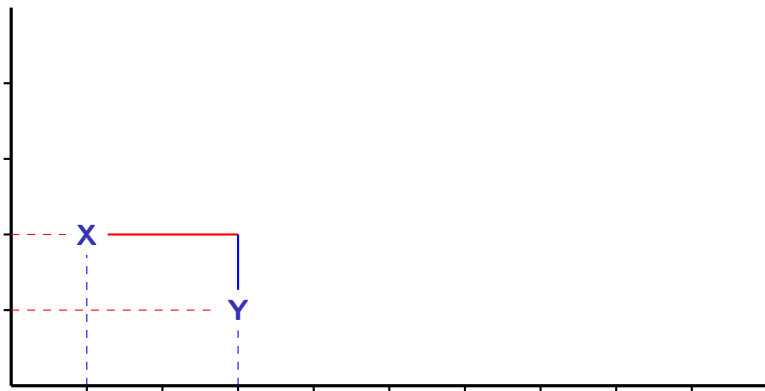
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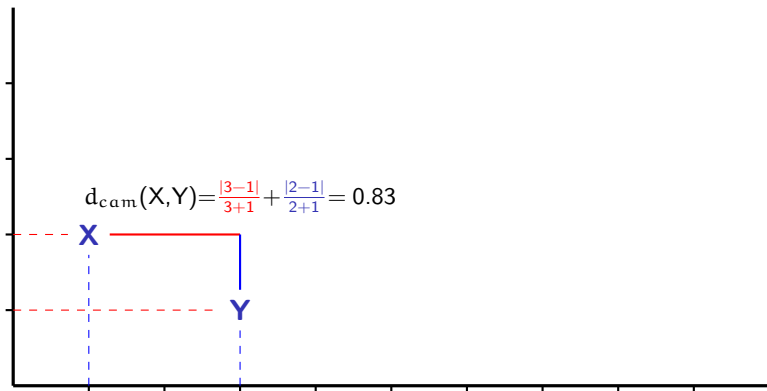
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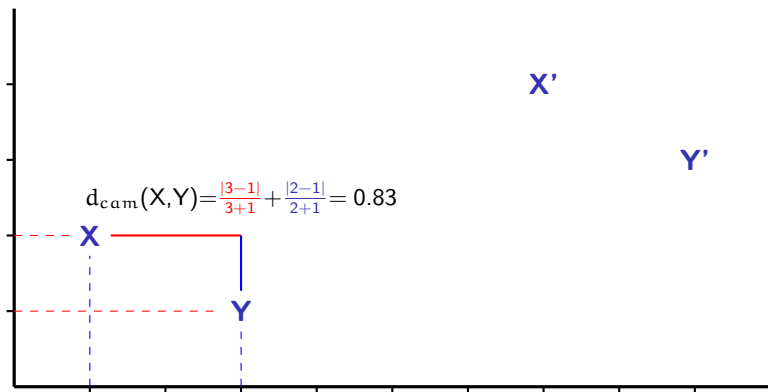
$$d_{\text{cam}}(X, Y) = \frac{|3-1|}{3+1} + \frac{|2-1|}{2+1} = 0.83$$



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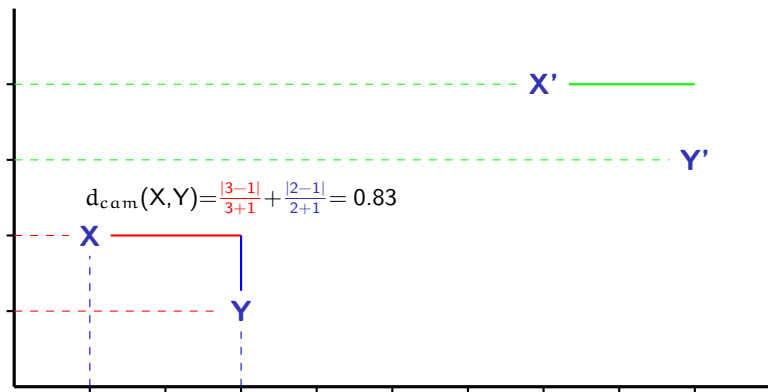
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Vector similarities/distances

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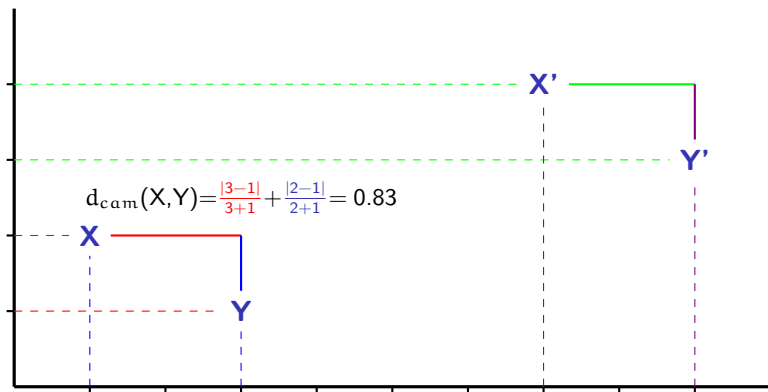
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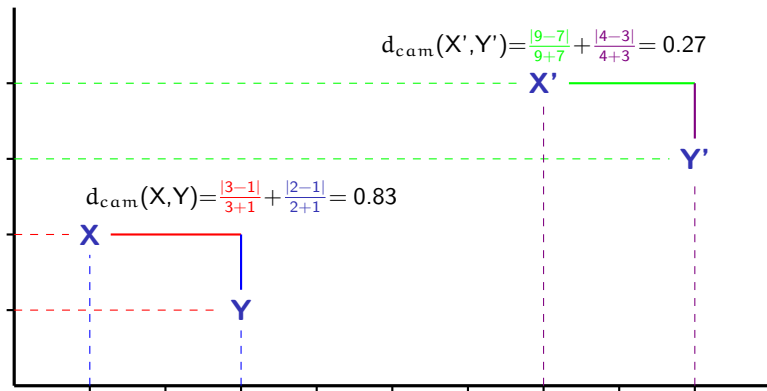
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Example

s_1 = Spokesman confirms senior government advisor was shot

s_2 = The spokesman said the senior advisor was shot dead

s_3 = Spokesman said the shot government advisor was dead

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	Spokesman	confirms	said	the	senior	government	advisor	was	shot	dead
s_1	1	1	0	0	1	1	1	1	1	0
s_2	1	0	1	2	1	0	1	1	1	1
s_3	1	0	1	1	0	1	1	1	1	1

	d_{man}	d_{euc}	d_{che}	d_{cam}	sim_{dot}	sim_{cos}
$s_1 \leftrightarrow s_2$	6	$\sqrt{8} = 2.83$	2	5	5	$\frac{5}{\sqrt{7}\sqrt{11}} = 0.57$
$s_1 \leftrightarrow s_3$	5	$\sqrt{5} = 2.24$	1	5	5	$\frac{5}{\sqrt{7}\sqrt{8}} = 0.67$
$s_2 \leftrightarrow s_3$	3	$\sqrt{3} = 1.73$	1	2.33	8	$\frac{8}{\sqrt{8}\sqrt{11}} = 0.85$

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Similarity
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Edit Distances

Vector/Set
similarities
and distances

Set similarities and
distances

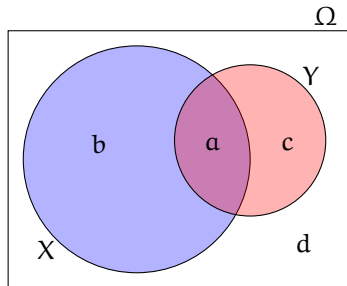
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Set similarities/distances

- When objects are represented as [feature] sets (or binary-valued vectors) we can use set similarity measures
- These similarities are in $[0, 1]$ and can be converted to distances simply subtracting: $d(X, Y) = 1 - \text{sim}(X, Y)$
- Easily computable using a contingency table:

		Y		
		1	0	
X	1	a	b	a + b
	0	c	d	c + d
		a + c	b + d	



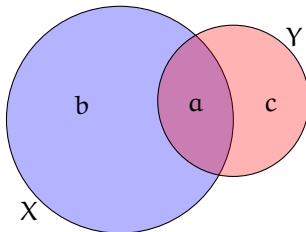
Set similarities/distances

■ Dice.

$$\text{sim}_{\text{dic}}(X, Y) = \frac{2 \cdot |X \cap Y|}{|X| + |Y|} = \frac{2a}{2a + b + c}$$

■ Jaccard.

$$\text{sim}_{\text{jac}}(X, Y) = \frac{|X \cap Y|}{|X \cup Y|} = \frac{a}{a + b + c}$$



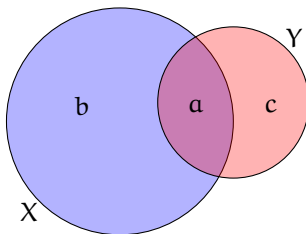
Set similarities/distances

■ Overlap.

$$\text{sim}_{\text{ovl}}(X, Y) = \frac{|X \cap Y|}{\min(|X|, |Y|)} = \frac{a}{\min(a + b, a + c)}$$

■ Cosine.

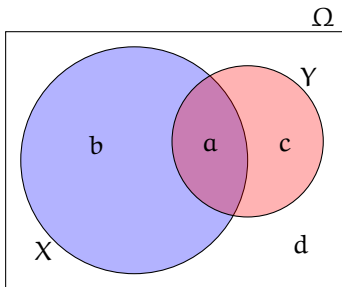
$$\text{sim}_{\text{cos}}(X, Y) = \frac{|X \cap Y|}{\sqrt{|X|} \cdot \sqrt{|Y|}} = \frac{a}{\sqrt{(a + b)} \sqrt{(a + c)}}$$



Set similarities/distances

■ Matching Coefficient

$$\text{sim}_{\text{mc}}(X, Y) = \frac{|X \cap Y| + |(\Omega - X) \cap (\Omega - Y)|}{|\Omega|} = \frac{a + d}{a + b + c + d}$$



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Example

s_1 = Spokesman confirms senior government advisor was shot

s_2 = The spokesman said the senior advisor was shot dead

s_3 = Spokesman said the shot government advisor was dead

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	Spokesman	confirms	said	the	senior	government	advisor	was	shot	dead
s_1	1	1	0	0	1	1	1	1	1	0
s_2	1	0	1	1	1	0	1	1	1	1
s_3	1	0	1	1	0	1	1	1	1	1

	sim_{dic}	sim_{jac}	sim_{ovl}	sim_{cos}	sim_{mc}
$s_1 \leftrightarrow s_2$	0.33	0.50	0.71	0.67	0.50
$s_1 \leftrightarrow s_3$	0.33	0.50	0.71	0.67	0.50
$s_2 \leftrightarrow s_3$	0.87	0.78	0.87	0.87	0.80

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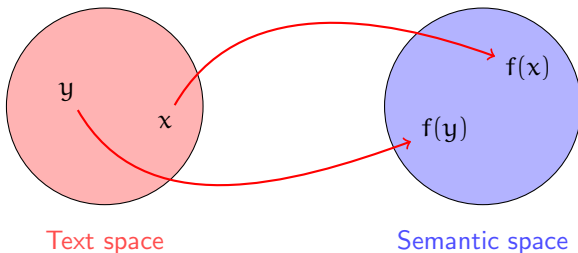
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Knowledge-based Approaches

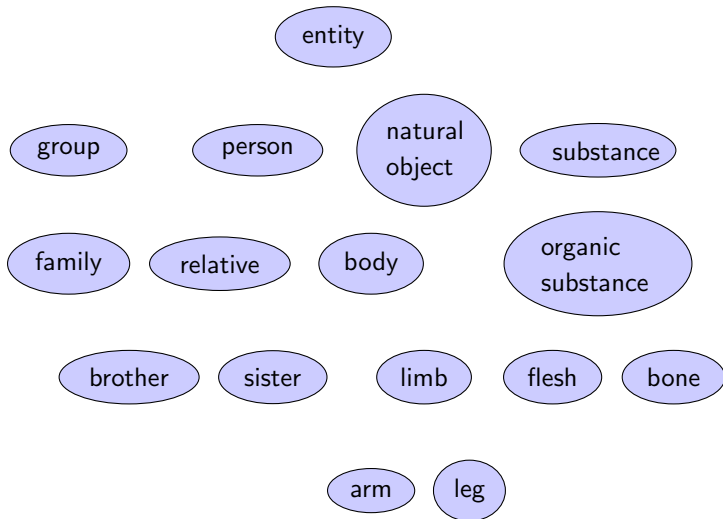
Project objects onto a knowledge-based semantic space:

$$d(x, y) = d_{\text{sem}}(f(x), f(y))$$



- Semantic spaces may be ontologies (e.g. WordNet, CYC, SUMO, ...) or graph-shaped knowledge bases (e.g. Wikipedia, DBpedia, ...).
- Projection function $f(x)$ is not trivial, since each word may map to more than one concept in semantic space.

WordNet



Similarity
Models

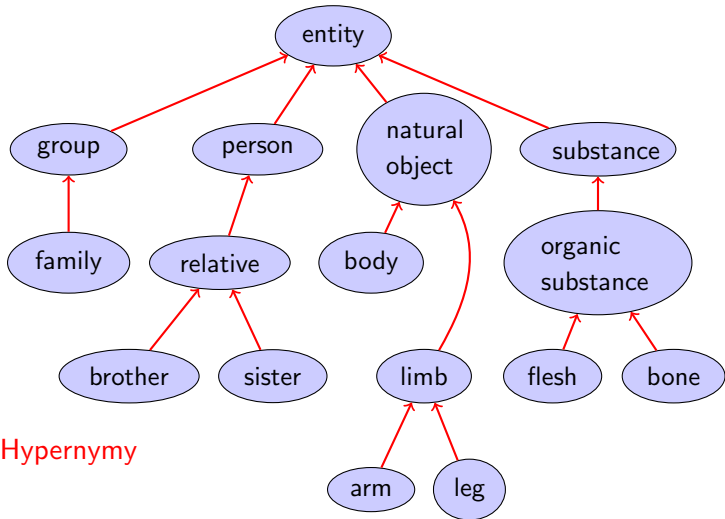
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Hypernymy

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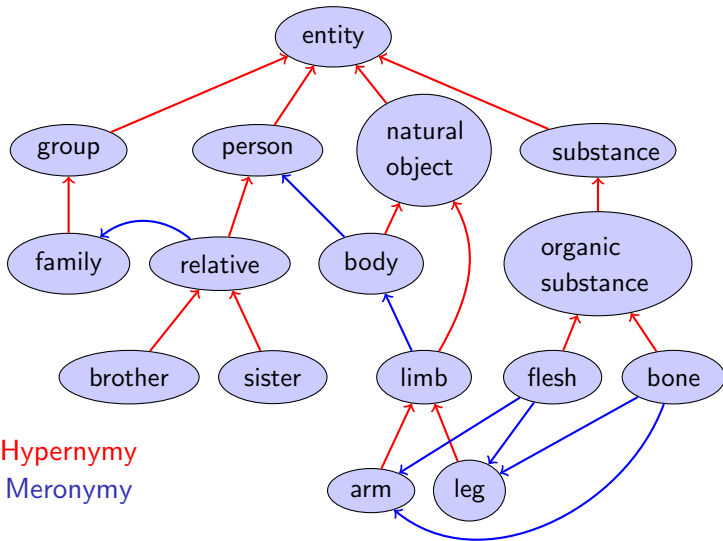
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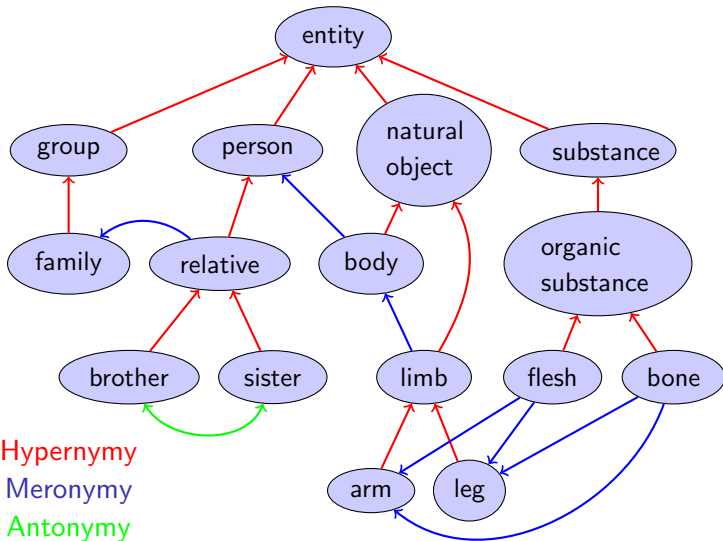
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Hypernymy

Meronymy

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WordNet distances

Based on graph structure:

- Shortest Path Length:

$$d(s_1, s_2) = \text{SPL}(s_1, s_2)$$

- Leacock & Chodorow (similarity, $[0, \infty)$):

$$s(s_1, s_2) = -\log \frac{\text{SPL}(s_1, s_2)}{2 \cdot \text{MaxDepth}}$$

- Wu & Palmer (similarity, $(0, 1]$):

$$d(s_1, s_2) = \frac{2 \cdot \text{depth}(\text{LCS}(s_1, s_2))}{\text{depth}(s_1) + \text{depth}(s_2)}$$

([LCS](#): Lowest Common Subsumer)

WordNet distances

Based on Information Content

$$IC(c) = -\log P(c) = -\log \frac{\text{freq}(c)}{N}$$

$\text{freq}(c)$: number of occurrences of *any instance* of concept c .

N : total number of observed instances.

- Resnik (similarity, $[0, \infty)$)

$$s(s_1, s_2) = IC(LCS(s_1, s_2))$$

- Jiang & Conrath (distance, $[0, \infty)$)

$$d(s_1, s_2) = IC(s_1) + IC(s_2) - 2 \cdot IC(LCS(s_1, s_2))$$

- Lin (similarity, $[0, 1]$):

$$s(s_1, s_2) = \frac{2 \cdot IC(LCS(s_1, s_2))}{IC(s_1) + IC(s_2)}$$

WordNet distances

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Based on sense information (not relations/structure)

- Gloss overlap: Any vector/set similarity measure applied to words in sense glosses.

Distances in Wikipedia

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- Graph-based distances (e.g Shortest Path Length, Page Rank, ...)
- Link-based similarities (some set similarity measure applied to the set of links of each page)
- Category-based similarities (some set similarity measure applied to the set of categories of each page)
- Text-based similarities (some text similarity measure applied to the texts of the pages)
- Heterogenous measures (combining several of the above in a weighted average)

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Corpus based representations

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Vectors to represent linguistic objects may be build using the distributional behaviour of the contexts they appear in.

E.g.:

- Represent words depending on the distribution of words frequently appearing nearby.
- Represent documents depending on the [general] distribution of words they contain.

Large corpus are required to pre-compute this distributions.

Corpus based representations

Vectors representing words or document contexts can be obtained in a variety of ways.

- Sparse vector representations
 - PMI
 - TF-IDF
- Dense vector representations
 - LSI
 - LDA
 - Word Embeddings

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Sparse vector
representations

PMI - Pointwise Mutual Information

- Mutual Information of two random variables X , Y measures the amount of information about one random variable obtained observing the other.

$$MI(X, Y) = \sum_{x \in X} \sum_{y \in Y} P(x, y) \log \frac{P(x, y)}{P(x)P(y)}$$

- Pointwise MI measures the ratio between the expected co-occurrence of events x and y , and their actual co-occurrence.

$$PMI(x, y) = \log \frac{P(x, y)}{P(x)P(y)}$$

Term-Term Matrix

PMI (or any other term-term relatedness feature, e.g. co-occurrence frequency) may be used to build a Term-Term Matrix.

Co-occurrence is typically defined as *co-occurrence in a window of size n* . In this example $n = 2$ (i.e. we count only consecutive words co-occurrences).

d_1 : "Two for tea and tea for two"

d_2 : "Tea for me and for you"

d_3 : "You and me for tea"

	two	for	tea	and	me	you	#occ.
two	0	2	0	0	0	0	2
for	-	0	4	1	2	1	5
tea	-	-	0	2	0	0	4
and	-	-	-	0	2	1	3
me	-	-	-	-	0	0	2
you	-	-	-	-	-	0	2

size-2 window co-occurrence absolute frequency term-term matrix

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Term-Term Matrix
(using PMI)

Term-Term Matrix

We need to compute the occurrence probability of a single word $P(x)$, and the co-occurrence probability of two words $P(x, y)$.

d_1 : "Two for tea and tea for two"

d_2 : "Tea for me and for you"

d_3 : "You and me for tea"

Total words: 18

Total size-2 windows: 15

$P(x, y)$	two	for	tea	and	me	you	$P(x)$
two	0	2/15	0	0	0	0	2/18
for	-	0	4/15	1/15	2/15	1/15	5/18
tea	-	-	0	2/15	0	0	4/18
and	-	-	-	0	2/15	1/15	3/18
me	-	-	-	-	0	0	2/18
you	-	-	-	-	-	0	2/18

size-2 window co-occurrence probability term-term matrix

Term-Term Matrix

We can compute PMI for each pair, obtaining a PMI Term-Term Matrix

d_1 : "Two for tea and tea for two"

d_2 : "Tea for me and for you"

d_3 : "You and me for tea"

Total words: 18

Total bigrams: 15

PMI(x, y)	two	for	tea	and	me	you	P(x)
two	$-\infty$	2.11	$-\infty$	$-\infty$	$-\infty$	$-\infty$	0.11
for	-	$-\infty$	2.11	0.53	2.11	1.11	0.28
tea	-	-	$-\infty$	1.85	$-\infty$	$-\infty$	0.22
and	-	-	-	$-\infty$	2.85	0.56	0.17
me	-	-	-	-	$-\infty$	$-\infty$	0.11
you	-	-	-	-	-	$-\infty$	0.11

PMI term-term matrix

Term-Term Matrix

- Entries in the Term-Term Matrix can directly be used to compare two terms (higher PMI - higher relatedness)
- Rows (or columns) in the Matrix can be used as term representations, and compared with vector similarity measures (to find terms with similar co-occurrence patterns).
- Negative PMI represent terms that *repel* each other (co-occur less than expected).
- Very low frequency terms may have negative PMI just because they have less chances to co-occur.
- Negative PMI values are often replaced by zero (PPMI - Positive PMI)

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Term-Term Matrix
(using PMI)

TF-IDF

TF-IDF (*Term Frequency* \times *Inverse Document Frequency*) is a measure of relevance (or relatedness) between a term and a document, very commonly used in Information Retrieval.

$$\text{TF-IDF}(t, d, \mathcal{D}) = \text{TF}(t, d) \times \text{IDF}(t, \mathcal{D})$$

where:

- \mathcal{D} is a collection (set) of documents, $\mathcal{D} = \{d_1, d_2, \dots, d_n\}$
- $d_i \in \mathcal{D}$ is a document, represented as a multiset (i.e. set with repetitions) of terms, $d_i = \{t_1, t_2, \dots, t_{m_i}\}$
- t is a term that may appear (or not) in documents in \mathcal{D} .

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Term-Document
Matrix (using
TF-IDF)

TF-IDF

- $TF(t, d)$: Frequency of a term t in a document d , relative to the length of the document

$$TF(t, d) = \frac{|\{x \in d : x = t\}|}{|d|}$$

- $IDF(t, \mathcal{D})$: Inverse of the proportion of documents containing term t in a document collection \mathcal{D} .

$$IDF(t, \mathcal{D}) = \log \left(\frac{|\mathcal{D}|}{|\{d \in \mathcal{D} : t \in d\}|} \right)$$

TF-IDF score for a term t and a document d is rewarded when the term is frequent in the document (high TF), and is penalized when the term appears in many documents (low IDF).

TF-IDF

There is not a **unique** TF-IDF.

- Alternative formulas may be used to compute term frequency (TF):
 - Raw count: $TF(t, d) = |\{x \in d : x = t\}|$
 - Binary frequency: $TF(t, d) = 1$ if $x \in d$, otherwise 0
 - Log normalization: $TF(t, d) = \log(1 + |\{x \in d : x = t\}|)$
 - double normalization:
$$TF(t, d) = K + (1 - K) \frac{|\{x \in d : x = t\}|}{\max_{t' \in d} |\{x \in d : x = t'\}|}$$
- Alternative formulas may be used to compute inverse document frequency (IDF):
 - Smoothed: $IDF(t, \mathcal{D}) = \log\left(\frac{|\mathcal{D}|}{1 + |\{d \in \mathcal{D} : t \in d\}|}\right) + 1$
 - Probabilistic: $IDF(t, \mathcal{D}) = \log\left(\frac{|\mathcal{D}| - |\{d \in \mathcal{D} : t \in d\}|}{|\{d \in \mathcal{D} : t \in d\}|}\right)$

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Term-Document Matrix

TF-IDF (or any other term-document relatedness measure, e.g. plain frequency) can be used to build a Term-Document Matrix:

d_1 : "Two for tea and tea for two"

d_2 : "Tea for me and for you"

d_3 : "You and me for tea"

	two	for	tea	and	me	you	$ d_i $
d_1	2	2	2	1	0	0	7
d_2	0	2	1	1	1	1	6
d_3	0	1	1	1	1	1	5

Absolute frequency term-document matrix

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TF-IDF (or any other term-document relatedness measure, e.g. plain frequency) can be used to build a Term-Document Matrix:

d_1 : “Two for tea and tea for two”

d_2 : “Tea for me and for you”

d_3 : “You and me for tea”

	two	for	tea	and	me	you	$ d_i $
d_1	2/7	2/7	2/7	1/7	0	0	7
d_2	0	2/6	1/6	1/6	1/6	1/6	6
d_3	0	1/5	1/5	1/5	1/5	1/5	5

TF term-document matrix

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Term-Document Matrix

TF-IDF (or any other term-document relatedness measure, e.g. plain frequency) can be used to build a Term-Document Matrix:

d_1 : “Two for tea and tea for two”

d_2 : “Tea for me and for you”

d_3 : “You and me for tea”

two	for	tea	and	me	you
$\log(3/1)$	$\log(3/3)$	$\log(3/3)$	$\log(3/3)$	$\log(3/2)$	$\log(3/2)$
= 1.58	= 0	= 0	= 0	= 0.58	= 0.58

IDF for each term in the collection

Term-Document Matrix

TF-IDF (or any other term-document relatedness measure, e.g. plain frequency) can be used to build a Term-Document Matrix:

d_1 : "Two for tea and tea for two"

d_2 : "Tea for me and for you"

d_3 : "You and me for tea"

	two	for	tea	and	me	you
d_1	$2/7 \cdot 1.58$	$2/7 \cdot 0$	$2/7 \cdot 0$	$1/7 \cdot 0$	$0 \cdot 0.58$	$0 \cdot 0.58$
d_2	$0 \cdot 1.58$	$2/6 \cdot 0$	$1/6 \cdot 0$	$1/6 \cdot 0$	$1/6 \cdot 0.58$	$1/6 \cdot 0.58$
d_3	$0 \cdot 1.58$	$1/5 \cdot 0$	$1/5 \cdot 0$	$1/5 \cdot 0$	$1/5 \cdot 0.58$	$1/5 \cdot 0.58$

TF-IDF term-document matrix

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Term-Document Matrix

TF-IDF (or any other term-document relatedness measure, e.g. plain frequency) can be used to build a Term-Document Matrix:

d_1 : "Two for tea and tea for two"

d_2 : "Tea for me and for you"

d_3 : "You and me for tea"

	two	for	tea	and	me	you	$ d_i $
d_1	0.45	0	0	0	0	0	7
d_2	0	0	0	0	0.097	0.097	6
d_3	0	0	0	0	0.117	0.117	5

TF-IDF term-document matrix

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Term-Document Matrix

TF-IDF table entries contain the *relevance* (or *relatedness*, or *similarity*, ...) between terms and documents, and can be used for IR.

- A query with the term *two* will retrieve document *d₁* with high relevance.
- A query with the term *me* or *you* will retrieve documents *d₂* and *d₃* with moderate relevance.
- Terms *for*, *and*, or *tea* would be filtered out from the index.

	two	for	tea	and	me	you	d _i
d ₁	0.45	0	0	0	0	0	7
d ₂	0	0	0	0	0.097	0.097	6
d ₃	0	0	0	0	0.117	0.117	5

TF-IDF term-document matrix

Term-Document Matrix

The Term-Document matrix may also be used as a representation of terms/documents:

- Row vectors in the matrix represent documents.

We can use vector distances/similarities to compare row vectors and find similar documents.

- Column vectors in the matrix represent terms.

We can use vector distances/similarities to compare column vectors and find similar terms.

Term-Document Matrix

In the running example:

- Documents d_2 and d_3 are similar documents, quite different from d_1 .
- Terms *me* and *you* behave similarly (wrt the documents where they appear).
- Terms *and*, *for*, and *tea* behave similarly (wrt the documents where they appear).

	two	for	tea	and	me	you	$ d_i $
d_1	0.45	0	0	0	0	0	7
d_2	0	0	0	0	0.097	0.097	6
d_3	0	0	0	0	0.117	0.117	5

TF-IDF term-document matrix

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Sparse vs. Dense Representations

Term-Term and Term-Document Matrices are typically sparse:

- A term co-occurs with only a small subset of all possible terms.
- A document contains only a small subset of all possible terms.

Dense representations are preferred:

- Lower dimensionality spaces, less features to deal with.
- Better generalization:
E.g., better handling of synonyms (*car* and *automobile* are different dimensions in a sparse representation, but may be combined into one dimension in a dense representation.)

Dimensionality Reduction

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To obtain dense representations, a dimensionality reduction must be performed.

Distributional semantics methods are appropriate:

- Latent Semantic Analysis (LSA, a.k.a. Latent Semantic Indexing, LSI)
- Word Embeddings

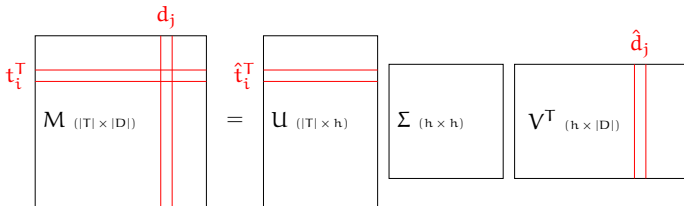
Latent Semantic Analysis

Goal: Reduce dimensionality of Term-Document matrix M .

Method: Apply SVD (Singular Value Decomposition):

$$M = U\Sigma V^T$$

basically, apply PCA (Principal Component Analysis) to Term-Document co-occurrence matrices.

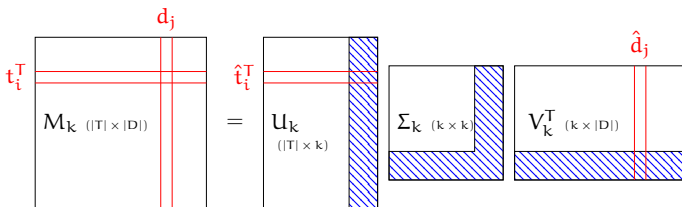


Σ is a diagonal matrix containing the **singular values**, and U, V are **orthonormal matrices** ($UU^T = U^TU = I$; $VV^T = V^TV = I$)

Latent Semantic Analysis (2)

Reduce M rank selecting the k largest singular values, obtaining M_k , a low-rank approximation of M :

$$M \approx M_k = U_k \Sigma_k V_k^T$$



Similarity
Models

Edit Distances

Vector/Set
similarities
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representa-
tions

LSA

Latent Semantic Analysis (3)

We can then compute low rank representations for document and term vectors:

- low-rank term vector: $\hat{t}_i = \Sigma_k^{-1} V_k^T t_i$ (see proof 1)
- low-rank document vector: $\hat{d}_j = \Sigma_k^{-1} U_k^T d_j$ (see proof 2)

And use them to compute similarities:

- Term-term similarity: Entry ij in $M_k M_k^T$, i.e. dot product of $\Sigma_k \hat{t}_i$ and $\Sigma_k \hat{t}_j$ (see proof 3)
- Doc-doc similarity: Entry ij in $M_k^T M_k$, i.e. dot product of $\Sigma_k \hat{d}_i$ and $\Sigma_k \hat{d}_j$ (see proof 4)
- Query-doc similarity: Convert query (seen as a mini-document vector) to low-rank space $\hat{q} = \Sigma_k^{-1} U_k^T q$ and compare with known documents.

Latent Semantic Analysis (proofs)

■ Proof 1:

$$\mathbf{t}_i^T = \hat{\mathbf{t}}_i^T \Sigma_k \mathbf{V}_k^T \rightarrow \mathbf{t}_i^T \mathbf{V}_k = \hat{\mathbf{t}}_i^T \Sigma_k \rightarrow \mathbf{t}_i^T \mathbf{V}_k \Sigma_k^{-1} = \hat{\mathbf{t}}_i^T \rightarrow \hat{\mathbf{t}}_i = \Sigma_k^{-1} \mathbf{V}_k^T \mathbf{t}_i$$

■ Proof 2:

$$\mathbf{d}_j = \mathbf{U}_k \Sigma_k \hat{\mathbf{d}}_j \rightarrow \mathbf{U}_k^T \mathbf{d}_j = \Sigma_k \hat{\mathbf{d}}_j \rightarrow \Sigma_k^{-1} \mathbf{U}_k^T \mathbf{d}_j = \hat{\mathbf{d}}_j$$

■ Proof 3:

$$\begin{aligned} \mathbf{M}_k \mathbf{M}_k^T &= \mathbf{U}_k \Sigma_k \mathbf{V}_k^T (\mathbf{U}_k \Sigma_k \mathbf{V}_k^T)^T = \mathbf{U}_k \Sigma_k \mathbf{V}_k^T (\mathbf{V}_k \Sigma_k^T \mathbf{U}_k^T) = \\ &= \mathbf{U}_k \Sigma_k \mathbf{I} \Sigma_k^T \mathbf{U}_k^T = \mathbf{U}_k \Sigma_k (\mathbf{U}_k \Sigma_k)^T \end{aligned}$$

Thus, element ij in the matrix is:

$$\mathbf{t}_i^T \Sigma_k (\mathbf{t}_j^T \Sigma_k)^T = \mathbf{t}_i^T \Sigma_k \Sigma_k^T \mathbf{t}_j = \Sigma_k^T \mathbf{t}_i \Sigma_k^T \mathbf{t}_j = \Sigma_k \mathbf{t}_i \Sigma_k \mathbf{t}_j$$

■ Proof 4:

$$\begin{aligned} \mathbf{M}_k^T \mathbf{M}_k &= (\mathbf{U}_k \Sigma_k \mathbf{V}_k^T)^T \mathbf{U}_k \Sigma_k \mathbf{V}_k^T = (\mathbf{V}_k \Sigma_k^T \mathbf{U}_k^T) \mathbf{U}_k \Sigma_k \mathbf{V}_k^T = \\ &= \mathbf{V}_k \Sigma_k^T \mathbf{I} \Sigma_k \mathbf{V}_k^T = \mathbf{V}_k \Sigma_k \Sigma_k^T \mathbf{V}_k^T = \mathbf{V}_k \Sigma_k (\mathbf{V}_k \Sigma_k)^T \end{aligned}$$

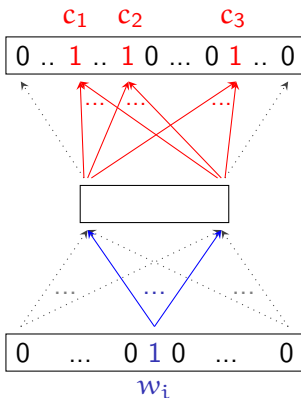
Thus, element ij in the matrix is:

$$\mathbf{d}_i^T \Sigma_k (\mathbf{d}_j^T \Sigma_k)^T = \mathbf{d}_i^T \Sigma_k \Sigma_k^T \mathbf{d}_j = \Sigma_k^T \mathbf{d}_i \Sigma_k^T \mathbf{d}_j = \Sigma_k \mathbf{d}_i \Sigma_k \mathbf{d}_j$$

Word Embeddings

Goal: Find a low-rank representation for terms.

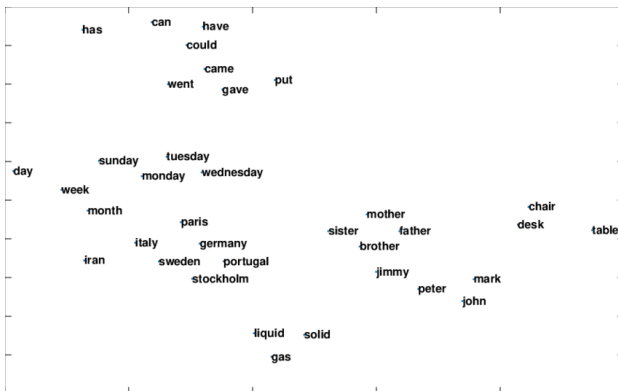
Method: Train a neural network to learn appropriate low-rank vectors for each term.



- Word w_i appearing near context words c_1, c_2, c_3 is used as a training example.
- The NN learns to relate words to their usual context words.
- The hidden layer input weights encode the usual contexts of each input word.
- Words usually appearing in similar context will have similar hidden layer weights.

LSA vs Word Embeddings

Distributional semantics methods produce close vectors for words in similar contexts.



Source: Ali Basirat 2018, *Principal Word Vectors*, PhD Thesis, Uppsala Univ.

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LSA vs Word Embeddings

■ LSA

- Allows comparing not only words, but also documents
- Requires managing documents
- Traditionally used in IR

■ WE

- Allows comparing only words, but not documents (may be tricked to, though)
- No need to manage/represent documents
- Learned vectors show analogy properties (man \rightarrow king, woman \rightarrow X?)
- Natural approach when using NN

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