Cerca i Anàlisi d'Informació (CAI)
Grau en Ciència i Enginyeria de Dades, UPC

Session 1: Introduction. Preprocessing. Text Statistics

Exercise List, Fall 2019

Basic comprehension questions. Check that you can answer them before proceeding.

1. Tell five Information Retrieval Systems you frequently use.
2. Tell the typical sequence of transformations we apply to a text while preprocessing and before adding to the index.
3. Tell the difference between stemming and lemmatizing.
4. Zipf's law tells the relation between X and Y. What are X and Y?
5. Heaps' law tells the relation between X and Y. What are X and Y?

Exercise 1

Guess (without using any software) what a text preprocessor could give on this text if it performs stopword removal and stemming:

> *We found my lady with no light in the room but the reading-lamp. The shade was screwed down so as to over-shadow her face. Instead of looking up at us in her usual straightforward way, she sat close at the table, and kept her eyes fixed obstinately on an open book.*
> *"Officer," she said, "it is important to the inquiry you are conducting to know beforehand if any person now in this house wishes to leave it?"*
> (William Wilkie Collins, *The Mooonstone*, Chapter 16)

Exercise 2

Suppose that our document retrieval system lets us enter a query, which is a set of words, and returns the set of documents that contain *all* the words in the query.

Imagine that we configure the system in four different modes, and we ask four times the same query.

- Mode 1: We don't remove stopwords and we don't stem neither documents nor queries. Let A_1 be the set of returned documents.
- Mode 2: We don't remove stopwords, but we stem both documents and queries. Let A_2 be the set of returned documents.
- Mode 3: We remove stopwords, but don't stem. Let A_3 be the set of returned documents.
- Mode 4: We remove stopwords, and then we stem both documents and queries. Let A_4 be the set of returned documents.

What relations can you prove among A_1, A_2, A_3, and A_4? For example, is $A_1 = A_2$? Is A_2 a subset of A_4?, etc.

Exercise 3

We have a document collection with a total of N word occurrences (N is large). We are told that it follows a Zipf's law of the form $frequence = c \cdot rank^{-\alpha}$.

1. What is c if $\alpha = 2$?
2. And if $\alpha = 1$?
3. Assume again $\alpha = 2$. What is the frequency of the most common term?
4. And what is the frequency of the 100th most frequent term?
5. And (roughly) how many words have frequency 1?

Exercise 4

We have a document collection with a total of 10^6 term occurrences. Supposing that terms are distributed in the texts following a power law of the form

$$f_i \cong \frac{c}{(i+10)^2}$$

give estimates of (1) the number of occurrences of the most frequent term; (2) the number of occurrences of the 100-th most frequent term; (3) the number of words occurring more than 2 times. *Hint:* $\sum_{i=11}^{\infty} \frac{1}{i^2} \cong 0.095$.

Exercise 5

We are given a random sample of 10,000 documents from a collection containing 1,000,000 documents. We count the different words in this sample, and we find 5,000. Supposing that the collection satisfies Heaps' law with exponent 0.5, give a reasoned estimate of the number of different words you expect to find in the whole collection.

Exercise 6

Let us deduce Heaps' law from Zipf's law.

- Let a collection have N word occurrences, with the frequence f_i of the i-th most common word proportional to $i^{-\alpha}$, $\alpha > 1$.
- Figure out (from previous exercises) the proportionality constant.
- Estimate the rank i such that f_i is likely to be less than 1.
- Explain why this should roughly be the number of distinct words we expect to see in the collection.
- Deduce that this number is $k \cdot N^{\beta}$. Tell the values of k and β as a function of α.

[Note: The given formulation of Zipf's law cannot, for obvious reasons, be taken too literally: If for some large i we have $c \cdot i^{-\alpha} = 0.03$, it makes no sense to say that the ith word appears 0.03 times in the collection. More abstractly, one could imagine texts generated by some random process which assigns probability $P(w)$ to the event that a random position in the text contains the word w. Then the word with rank 1 is the w with highest $P(w)$, etc. Zipf's law is a statement about the form of the probability distribution P. One can then compute rigorously the expected number of distinct words in

a text of length N according to this probabilistic model. Let us just say that we this way we obtain the same β but a different k.]

[Note 2: It is also possible but a bit more involved to deduce a power law for word frequences (generalizing Zipf's law) from Heap's law]