Supervised methods: Introduction and evaluation

Mario Martin

UPC - Computer Science Dept. mmartin@cs.upc.edu http://www.cs.upc.edu/~mmartin/DM.htm

Outline



- Definition and examples
- Generalization
- 2 Evaluation of classifiers
 - Introduction and measures
 - Cross-validation
 - k-fold cross-validation and LOO
 - Bootstrapping
 - Confidence intervals

Definition and examples Generalization

Outline



- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation
- k-fold cross-validation and LOO
- Bootstrapping
- Confidence intervals

Definition and examples Generalization

Outline



- Definition and examples
- Generalization
- 2 Evaluation of classifiers
 - Introduction and measures
 - Cross-validation
 - k-fold cross-validation and LOO
 - Bootstrapping
 - Confidence intervals

Definition and examples Generalization

Supervised Learning definition

Definition

Given: A dataset D of observations, usually represented as a table where each row is an observation and each column a descriptor.

Goal: Learn to predict one column of the dataset, named *label*, for new data.

Definition and examples Generalization

Dataset example

🛅 Table (5 fields, 151 records) #2									
😰 File 🖻 Edit 🏷 Generate 🐻 🕒 📢 🏭 🕢 🖉 🗙									
	Table A	nnotations							
		Sepal_len_cm	Sepal_wid_cm	Petal_len_cm	Petal_wid_cm	Class			
	1	5.100	3.500	1.400	0.200	Iris-setosa		▲	
	2	4.900	3.000	1.400	0.200	Iris-setosa			
	3	4.700	3.200	1.300	0.200	Iris-setosa			
	4	4.600	3.100	1.500	0.200	Iris-setosa			
	5	5.000	3.600	1.400	0.200	Iris-setosa			
	6	5.400	3.900	1.700	0.400	Iris-setosa			
	7	4.600	3.400	1.400	0.300	Iris-setosa			
	8	5.000	3.400	1.500	0.200	Iris-setosa			
	9	4.400	2.900	1.400	0.200	Iris-setosa			
	10	4.900	3.100	1.500	0.100	Iris-setosa			
	11	5.400	3.700	1.500	0.200	Iris-setosa			
	12	4.800	3.400	1.600	0.200	Iris-setosa			
	13	4.800	3.000	1.400	0.100	Iris-setosa			
	14	4.300	3.000	1.100	0.100	Iris-setosa			
	15	5.800	4.000	1.200	0.200	Iris-setosa			
	4.0	5 700		4 500	0.400	a a 1 a 1 a 1 a 1 a 1 a 1 a 1 a 1 a 1 a			

Mario Martin

Supervised methods

Definition and examples Generalization

Supervised Learning examples

Some examples

- From a dataset of bank costumers, *predict* whether a new costumer will return a loan or not.
- From a dataset of images of digits, learn to *identify* the digit represented by a new image.
- From a dataset of emails, learn to *distinguish* between SPAM and not SPAM.
- From a dataset of Magnetoencephalography recordings of patients, *diagnose* whether a new individual is schizophrenic or not.

Definition and examples Generalization

Supervised Learning as Classification

• All the previous tasks were examples of *learning* (why?)

Definition and examples Generalization

Supervised Learning as Classification

• All the previous tasks were examples of *learning* (why?) to *classify* (a lot of tasks can be expressed as classification tasks)

Definition and examples Generalization

Supervised Learning as Classification

- All the previous tasks were examples of *learning* (why?) to *classify* (a lot of tasks can be expressed as classification tasks)
- Notice that labels are discrete values (in other case we are talking about *regression*)

Definition and examples Generalization

Supervised Learning as Classification

- All the previous tasks were examples of *learning* (why?) to *classify* (a lot of tasks can be expressed as classification tasks)
- Notice that labels are discrete values (in other case we are talking about *regression*)
- In order to classify an object in a right class, we need to build a *classifier*

Definition and examples Generalization

Supervised Learning constraints

Usual considerations:

- Dataset contains **positive** and **negative** examples for each labels.
- Examples are randomly sampled (i.i.d.).
- ... Other assumptions later on.

Definition and examples Generalization

Outline



- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation
- k-fold cross-validation and LOO
- Bootstrapping
- Confidence intervals

Definition and examples Generalization

Generalization

• How can we infer the class of one observation from other cases?

Definition and examples Generalization

- How can we infer the class of one observation from other cases?
- Generalization is the ability to extend knowledge of a dataset to new data

Definition and examples Generalization

- How can we infer the class of one observation from other cases?
- Generalization is the ability to extend knowledge of a dataset to new data
- But which is the source of the magic of generalization?

Definition and examples Generalization

- How can we infer the class of one observation from other cases?
- Generalization is the ability to extend knowledge of a dataset to new data
- But which is the source of the magic of generalization?



Definition and examples Generalization



Definition and examples Generalization



Definition and examples Generalization



Definition and examples Generalization



Definition and examples Generalization

Generalization

Overfitting

When the learning method is too flexible, there is risk of **overfitting** (the data)



Definition and examples Generalization

Generalization

Any learning method will show a tendency to *simple explanations* for data:

- Shortest description:
 - Minimum description length
 - Shortest tree size
 - Fewest parameters model
 - Independence of columns
- Regularization about complexity of the classifier:
 - Values of parameters (f.i. limited weight in neural networks)
 - Trade-off on capacity of classifier and error

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Outline



- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation
- k-fold cross-validation and LOO
- Bootstrapping
- Confidence intervals

Introduction and measures

Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Outline



- Definition and examples
- Generalization

2 Evaluation of classifiers

Introduction and measures

- Cross-validation
- k-fold cross-validation and LOO
- Bootstrapping
- Confidence intervals

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Introduction

- Data mining in supervised mode has a target column.
- Differently than in the case of clustering, now we have an objective way to measure the success of classifiers: Test new cases with the classifier and check predicted labels with reality.

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Introduction

- Data mining in supervised mode has a target column.
- Differently than in the case of clustering, now we have an objective way to measure the success of classifiers: Test new cases with the classifier and check predicted labels with reality.
- But not so easy. There are a lot of different measures to qualify success of a classifier.

Introduction and measures

Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Measures



Definition Evaluation of classifiers Some observations Measures Measures Measures



Definition Evaluation of classifiers Some observations Confussion matrix

Given a classifier, asses the error it produces on a set of instances from the **confusion matrix**:

	Actually Positive	Actually Negative
Predicted Positive	True Positive cases (TP)	False Positive cases (FP)
Predicted Negative	False Negative cases(FN)	True Negative cases (TN)

Each entry is the number of instances.

Introduction and measures Cross-validation

Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Measures based on confusion matrix

	Actually Positive	Actually Negative
Predicted Positive	True Positive cases (TP)	False Positive cases (FP)
Predicted Negative	False Negative cases(FN)	True Negative cases (TN)

Accuracy

Accuracy: Empiric error on the set of cases given

$$Ac = \frac{TP + TN}{TP + TN + FP + FN}$$

Introduction and measures

Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Measures based on confusion matrix

Accuracy is not a good measure when:

- Unbalanced datasets
- Different costs for each kind of error

	Act. Pos.	Act. Neg.		Act. Pos.	Act. Neg.
Pred. Pos.	10	100	Pred. Pos.	50	140
Pred. Neg.	40	300	Pred. Neg.	0	260

Unbalanced case: Assume we are interested in detecting one kind of documents from a large corpus. Both tables same accuracy but show different behaviors.

Introduction and measures

Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Measures based on confusion matrix

Accuracy is not a good measure when:

- Unbalanced datasets
- Different costs for each kind of error

	Act. Pos.	Act. Neg.		Act. Pos.	Act. Neg.
Pred. Pos.	100	10	Pred. Pos.	100	100
Pred. Neg.	100	290	Pred. Neg.	10	290

Different costs: Assume cost of misclassifying a positive case is 10 times misclassifying a negative case. Same accuracy but different cost.

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Measures based on confusion matrix

Measures taken from document classification (imbalanced case)

• Recall: Proportion of positive cases that were detected

$$R = \frac{TP}{TP + FN}$$

• **Precision**: Proportion of positive cases with respect the number of cases labeled positive

$$P = \frac{TP}{TP + FP}$$

• F-measure: Harmonic mean of Recall and Precision

$$F = \frac{2}{\frac{1}{P} + \frac{1}{R}} = \frac{2PR}{P + R}$$

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

ROC curve

When the classifier can return *belief* in prediction, then we can obtain different predicitons by changing the cut-off point that separates examples. We can plot then the ROC curve (FP *vs.* TP rate).

• True Positive Rate (TPR):

$$TPR = rac{TP}{TP + FN}$$

• False Positive Rate (FPR):

$$FPR = \frac{TN}{TN + FP}$$

Introduction and measures

Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

ROC curve


Introduction and measures

Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

ROC curve



Mario Martin Supervised methods

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

ROC curve

When the classifier can return *belief* in prediction, then we can obtain different predicitons by changing the cut-off point that separates examples. We can plot then the ROC curve (FP *vs.* TP rate).



- Are Under Curve (AUC) measure to compare classifiers
- Interesting to find best threshold for classifier
- ...specially good for imbalanced data sets

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Outline



- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation
- k-fold cross-validation and LOO
- Bootstrapping
- Confidence intervals

3 Some observations

Definition Evaluation of classifiers Some observations Cross-validation and measures Cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

• Matrix confusion is generated form testing the classifier on new data.

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Cross-validation

- Matrix confusion is generated form testing the classifier on new data.
- Examples used for learning the classifier cannot be used to generate the matrix confusion (why?)

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Cross-validation

- Matrix confusion is generated form testing the classifier on new data.
- Examples used for learning the classifier cannot be used to generate the matrix confusion (why?)
- ... But how do we obtain new data?

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Cross-validation

- Matrix confusion is generated form testing the classifier on new data.
- Examples used for learning the classifier cannot be used to generate the matrix confusion (why?)
- ... But how do we obtain new data?

Solution

Do not use all your data for learning.... Keep some examples for testing!

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Cross-validation

Cross-validation: Divide your data in two sets - one for learning and one for testing

Definition Evaluation of classifiers Some observations Cross-validation and measures Cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Cross-validation: Divide your data in two sets - one for learning and one for testing



• Use more data for training than for testing. Usually 66% data for training - 33% of data testing

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Problems with cross-validation

- When data is scarce you "waste" your data for testing.
- More importantly, results may depend on the split of data into training and testing.

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Problems with cross-validation

- When data is scarce you "waste" your data for testing.
- More importantly, results may depend on the split of data into training and testing.
- How can we solve that?

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Problems with cross-validation

- When data is scarce you "waste" your data for testing.
- More importantly, results may depend on the split of data into training and testing.
- How can we solve that?
- ... repeating the split several times and averaging results.
 - k-fold cross-validation
 - leave-one-out
 - Bootstrapping

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Outline



- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation

• k-fold cross-validation and LOO

- Bootstrapping
- Confidence intervals

3 Some observations

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

k-fold cross-validation

k-fold cross-validation: Divide your dataset into k disjoints subsets of equal length.



Repeat k times the learning process, each time leaving out for testing a different subset.



Average the k accuracy estimators.

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

k-fold cross-validation

Advantages:

• More robust estimator (less variance)

Problems:

- \bullet We still waste 1/k of your data for testing
- We have to repeat the learning process k times

How do we set k? Trade-off time/variance. Usually set to 5 or 10.

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Leave-one-out (LOO)

Leave-one-out (LOO): Extreme version of k-fold cross-validation where k is set to n, the number of examples in your dataset.

Repeat *n* executions of the learning algorithm with n - 1 examples for learning and 1 for testing (every time a different one).

Average the n estimators.

Obviously it takes time to compute, but takes maximum profit of examples and reduces variance of estimator.

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Outline



- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation
- k-fold cross-validation and LOO

Bootstrapping

Confidence intervals

3 Some observations

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Bootstrapping

Repeat this process *K* times (hundreds!):

- Randomly select (with replacement) n examples for training
- Examples not selected for training are used for testing (number of examples is likely to change from fold to fold)

True error is estimated as the average error rate on test data

Complete dataset	(X_1) (X_2) (X_3) (X_4) (X_5)	
Experiment 1	(X_3) (X_1) (X_3) (X_3) (X_5)	(X_2) (X_4)
Experiment 2	(X_5) (X_5) (X_3) (X_1) (X_2)	(X ₄)
Experiment 3	(X_5) (X_5) (X_1) (X_2) (X_1)	(X_3) (X_4)
Experiment K	(X_3) (X_3) (X_3) (X_3) (X_3) Training sets	$\underbrace{\begin{pmatrix} x_{1} \\ x_{2} \end{pmatrix} \begin{pmatrix} x_{3} \\ x_{3} \end{pmatrix} \begin{pmatrix} x_{4} \\ x_{5} \end{pmatrix}}_{\text{Test sets}}$

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Outline

Definition

- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation
- k-fold cross-validation and LOO
- Bootstrapping
- Confidence intervals

3 Some observations

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Confidence interval one classifier

• $E_{\text{empirical}}$ (from now on $\hat{\epsilon}$) follows a binomial distribution (why?)

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Confidence interval one classifier

- $E_{\text{empirical}}$ (from now on $\hat{\epsilon}$) follows a binomial distribution (why?) with mean $\hat{\epsilon}$ and $\sigma = \sqrt{\frac{\hat{\epsilon} (1-\hat{\epsilon})}{n}}$
- When n ê (1 − ê) ≥ 5 binomial can be approximated by a Normal distribution with same mean and variance. So:

$$\hat{\epsilon} - z_{\alpha/2} \ \sigma \le \epsilon \le \hat{\epsilon} + z_{\alpha/2} \ \sigma$$

For a 95% confidence interval $z_{0.025} = 1.96$.

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Confidence interval one classifier

- $E_{\text{empirical}}$ (from now on $\hat{\epsilon}$) follows a binomial distribution (why?) with mean $\hat{\epsilon}$ and $\sigma = \sqrt{\frac{\hat{\epsilon} (1-\hat{\epsilon})}{n}}$
- When n ê (1 − ê) ≥ 5 binomial can be approximated by a Normal distribution with same mean and variance. So:

$$\hat{\epsilon} - z_{\alpha/2} \ \sigma \leq \epsilon \leq \hat{\epsilon} + z_{\alpha/2} \ \sigma$$

For a 95% confidence interval $z_{0.025} = 1.96$.

When n ê (1 − ê) < 5, apply cumulative distribution function of binomial: prob. of doing maximum k errors is Pr{X ≤ k} = ∑_{i=0}^k (ⁿ_i)êⁱ(1 − ê)^{n−i}.

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Confidence interval one classifier

- $E_{\text{empirical}}$ (from now on $\hat{\epsilon}$) follows a binomial distribution (why?) with mean $\hat{\epsilon}$ and $\sigma = \sqrt{\frac{\hat{\epsilon} (1-\hat{\epsilon})}{n}}$
- When n ê (1 − ê) ≥ 5 binomial can be approximated by a Normal distribution with same mean and variance. So:

$$\hat{\epsilon} - z_{\alpha/2} \ \sigma \leq \epsilon \leq \hat{\epsilon} + z_{\alpha/2} \ \sigma$$

For a 95% confidence interval $z_{0.025} = 1.96$.

When n ê (1 − ê) < 5, apply cumulative distribution function of binomial: prob. of doing maximum k errors is Pr{X ≤ k} = ∑_{i=0}^k (ⁿ_i)êⁱ(1 − ê)^{n−i}.

binom.test(k, n, e, "less", conf.level)

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Confidence interval of averaging k classifiers

Addition of Binomials can be approximated by Normal. So again:

$$\hat{\epsilon} - z_{lpha/2} \ \sigma \leq \epsilon \leq \hat{\epsilon} + z_{lpha/2} \ \sigma$$

But now, $\hat{\epsilon}$ is the average of all cross-validation runs and $\sigma = \sqrt{\frac{\hat{\epsilon} (1-\hat{\epsilon})}{n}}$ where *n* is the numbre of examples used in all cross-validation runs

Introduction and measures Cross-validation k-fold cross-validation and LOC Leave-one-out (LOO) Bootstrapping Confidence intervals

Comparing two classifiers: McNemar's Test

- Goal: decide which of two classifiers h₀ and h₁ has lower error rate
- Run h_0 and h_1 and build the following table:

n ₀₀ : number of cases	n ₀₁ : number of cases	
both right	h_0 right and h_1 fails	
<i>n</i> ₁₀ : number of cases	<i>n</i> ₁₁ : number of cases	
h_0 fails and h_1 right	both fail	

Introduction and measures Cross-validation k-fold cross-validation and LOO Leave-one-out (LOO) Bootstrapping Confidence intervals

Comparing two classifiers: McNemar's Test

- Null hypothesis: $n_{01} = n_{10}$ (both same error)
- McNemar's Test:

$$M = \frac{(|n_{01} - n_{10}| - 1)^2}{n_{01} + n_{10}} > \chi^2_{1,\alpha}$$

- M is distributed approximately as χ^2 with 1 degree of freedom. For a 95% confidence test, $\chi^2_{1,0.95} = 3.84$. So if M is larger than 3.84, then with 95% confidence, we can reject the null hypothesis
- Once we know they don't have the same error, which one is better?

Multi-class problem Dataset preparation Approaches to learn classifiers

Outline

Definition

- Definition and examples
- Generalization

2 Evaluation of classifiers

- Introduction and measures
- Cross-validation
- k-fold cross-validation and LOO
- Bootstrapping
- Confidence intervals

3 Some observations

Multi-class problem Dataset preparation Approaches to learn classifiers

Some observations:

- Multi-class classification
- 2 Data preparation
- **③** General approaches to build classifiers

Multi-class problem Dataset preparation Approaches to learn classifiers

Some observations:

Multi-class classification

- 2 Data preparation
- General approaches to build classifiers

Multi-class problem Dataset preparation Approaches to learn classifiers

Multi-class problem

Some observations:

- $\bullet\,$ In some classifiers labels are assumed to be binary: +1/-1
- We name *positive examples* to observations with label +1 and *negative examples* to observations with labels -1

When labels are not binary we always can build a combination of classifiers

Two approximations:

- One versus One (OVO)
- One versus All (OVA)

Multi-class problem Dataset preparation Approaches to learn classifiers

One Versus One

Given k labels, learn to separate class 1 from 2, class 1 from 3, ... class 1 from k, class 2 from 3, class 2 from 4, ... class 2 from k, class k - 1 from class k



Multi-class problem Dataset preparation Approaches to learn classifiers

One Versus One

Given k labels, learn to separate class 1 from 2, class 1 from 3, ... class 1 from k, class 2 from 3, class 2 from 4, ... class 2 from k, class k - 1 from class k



Multi-class problem Dataset preparation Approaches to learn classifiers

One Versus One

Given k labels, learn to separate class 1 from 2, class 1 from 3, ... class 1 from k, class 2 from 3, class 2 from 4, ... class 2 from k, class k - 1 from class k



Multi-class problem Dataset preparation Approaches to learn classifiers

One Versus One

After learning $\frac{k(k-1)}{2}$ classifiers, when label for a new observation is required, apply all classifiers and *vote*.

Ties are broken by randomly choosing one label.

Example:

Classifier	Vote
1 vs. 2	1
1 vs. 3	1
2 vs. 3	3

Final label: 1

Multi-class problem Dataset preparation Approaches to learn classifiers

One Versus All

Given k labels, learn to separate class 1 from all other classes, class 2 from all other classes class k - 1 from all other classes.



Multi-class problem Dataset preparation Approaches to learn classifiers

One Versus All

After learning k classifiers, when label for a new observation is required, apply all classifiers and *vote*.

Ties are broken by randomly choosing one label.

Example:

Classifier	Vote
1 vs. All	1
2 vs. All	All
3 vs. All	All

Final label: 1
Multi-class problem Dataset preparation Approaches to learn classifiers

Some comments:

- Multi-class classification
- 2 Data preparation
- General approaches to build classifiers

Multi-class problem Dataset preparation Approaches to learn classifiers

Dataset preparation

- No missing values.
- Relevant features included in dataset (with not an overwhelming amount of irrelevant columns).
- Some algorithms only work with numerical data or with categorical data.
- Usually, we work with normalized or standardized data.

Multi-class problem Dataset preparation Approaches to learn classifiers

Dataset preparation

- No missing values √.
- Relevant features included in dataset (with not an overwhelming amount of irrelevant columns).
- Some algorithms only work with numerical data or with categorical data.
- Usually, we work with normalized or standardized data.

Multi-class problem Dataset preparation Approaches to learn classifiers

Dataset preparation

- No missing values.
- **Relevant features included in dataset** (with not an overwhelming amount of irrelevant columns).
- Some algorithms only work with numerical data or with categorical data.
- Usually, we work with normalized or standardized data.

Multi-class problem Dataset preparation Approaches to learn classifiers

Relevant features

- Most algorithms work with a moderate amount of irrelevant columns. However, when the number of irrelevant columns is too much large, the algorithm can be fooled.
- Some methods remove irrelevant features (this is know as feature selection). For instance, sort features by some correlation measure with labels (Correlation, Information Gain, etc.) and keep the top ones.
- We'll see that in the next set of slides

Multi-class problem Dataset preparation Approaches to learn classifiers

Dataset preparation

- No missing values.
- Relevant features included in dataset (with not an overwhelming amount of irrelevant columns).
- Some algorithms only work with numerical data or with categorical data.
- Usually, we work with normalized or standardized data.

Multi-class problem Dataset preparation Approaches to learn classifiers

When numerical data is needed

• Build a new column for each category.

Object	Color
Obj1	blue
Obj2	green
Obj3	green
Obj4	red

Multi-class problem Dataset preparation Approaches to learn classifiers

When numerical data is needed

• Build a new column for each category.

Object	Color		Object	blue	green	red
Obj1	blue	\Rightarrow	Obj1	1	0	0
Obj2	green	\rightarrow	Obj2	0	1	0
Obj3	green		Obj3	0	1	0
Obj4	red		Obj4	0	0	1

Multi-class problem Dataset preparation Approaches to learn classifiers

When categorical data is needed

Discretization of continuous data. Several approaches:

- Rounding (Decimation)
- Finding best cut places
 - Minimize:

$$ER = \sum_{n=1}^{k} \left(\sum_{i \in bin_k} |v_{i,n} - v_{moda,n}| \right)$$

where k is the number of bins (categories). For instance {1, 1, 2, 2, 2, 5, 6, 8, 8, 9} into three bins: $A = \{1, 1, 2, 2, 2\}, B = \{5, 6\}, C = \{8, 8, 9\}$

• Target oriented methods: Look for the statistically best splitting of data according to label distribution, f.i., ChiMerge method

Multi-class problem Dataset preparation Approaches to learn classifiers

Dataset preparation

- No missing values.
- Relevant features included in dataset (with not an overwhelming amount of irrelevant columns).
- Some algorithms only work with numerical data or with categorical data.
- Usually, we work with normalized or standardized data.

Multi-class problem Dataset preparation Approaches to learn classifiers

Normalization and standardization

In order to give the same weight to all features we normalize the data to make them independent of units.

• Normalization 0,1:

$$v_i^n(k) = \frac{v_i(k) - \min(v_i)}{\max(v_i) - \min(v_i)}$$

Multi-class problem Dataset preparation Approaches to learn classifiers

Normalization and standardization

In order to give the same weight to all features we normalize the data to make them independent of units.

• Normalization 0,1:

$$v_i^n(k) = \frac{v_i(k) - \min(v_i)}{\max(v_i) - \min(v_i)}$$

• Standardization to mean 0, sigma 1

$$v_i^n(k) = \frac{v_i(k) - \mu(v_i)}{\sigma(v_i)}$$

Multi-class problem Dataset preparation Approaches to learn classifiers

Some comments:

- Multi-class classification
- 2 Data preparation
- **③** General approaches to build classifiers

Multi-class problem Dataset preparation Approaches to learn classifiers

Supervised Learning as Classification

How to determine the right label for a given data? Use of learning algorithms (or data mining algorithms)

Two different approaches:

- Discriminative methods
- Generative methods

Multi-class problem Dataset preparation Approaches to learn classifiers

Discriminative

Build a mechanism that allows to discriminate (separate) cases of different classes without any assumption about data



Multi-class problem Dataset preparation Approaches to learn classifiers

Generative

Assume a parametric distribution of data, learn the parameters for the distribution (model the classes) and, when needed, find the most likely class for new observations.

