



Parsing Chart Extensions ¹

- Chart extensions
- Dynamic programming methods
 - CKY
 - Earley

Parsing Chart Extensions ₂

- Constraint propagation
 - CSP (Quesada)
- Bidirectional chart parsing
 - Head driven
 - functors driven
 - Island driven
- Using Charts for unification-based formalisms
 - Restrictors
 - Backbone grammars

Parsing Chart Extensions ₃

Constraint propagation

- CSP J.F Quesada
- Grammar ambiguity (external) vs parser ambiguity (internal)
- 2 strategies:
 - Basic mechanism bidirectional BU
 - TD predictions
 - Partial derivations parciales
 - adjacencies
- Horizontal mechanism for constraint propagation

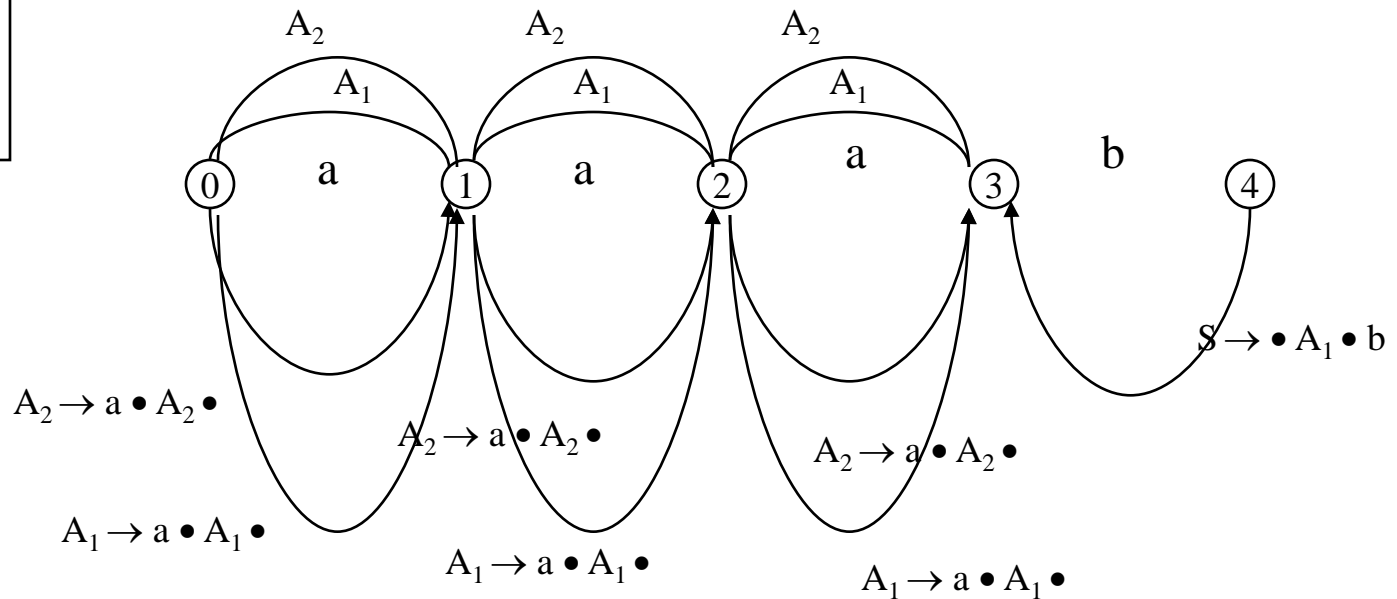
Parsing Chart Extensions 4

$S \rightarrow A_1 b$
 $S \rightarrow A_2 c$
 $A_1 \rightarrow a$
 $A_1 \rightarrow a A_1$
 $A_2 \rightarrow a$
 $A_2 \rightarrow a A_2$

grammar

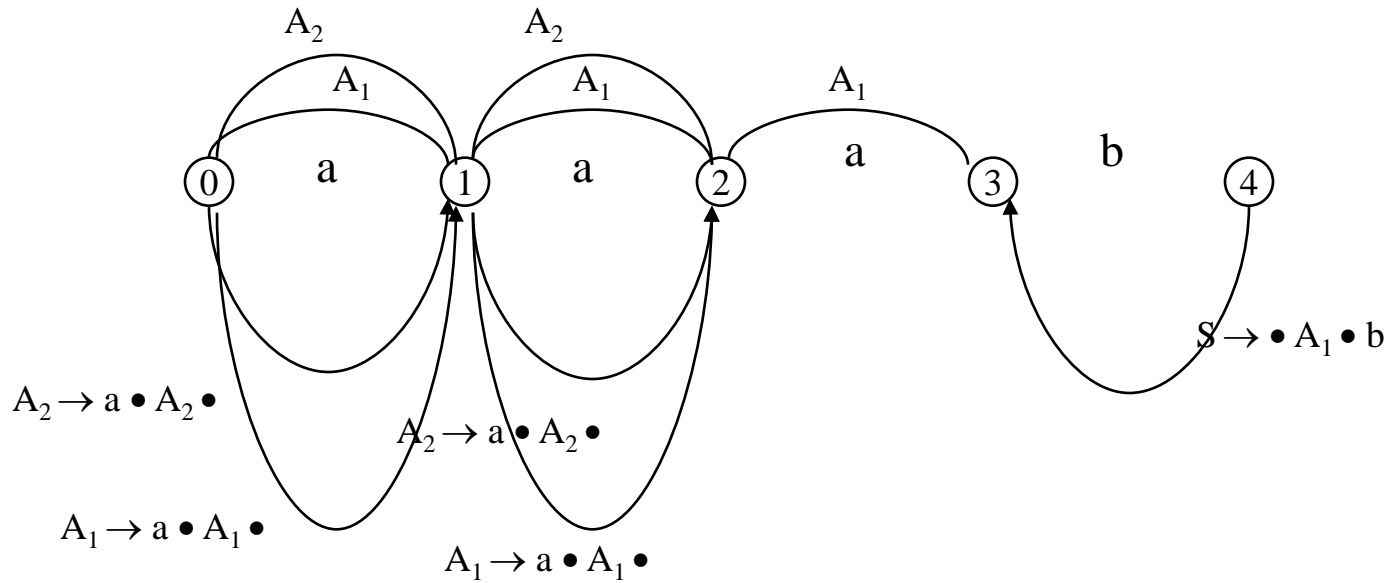
a a a b

sentence



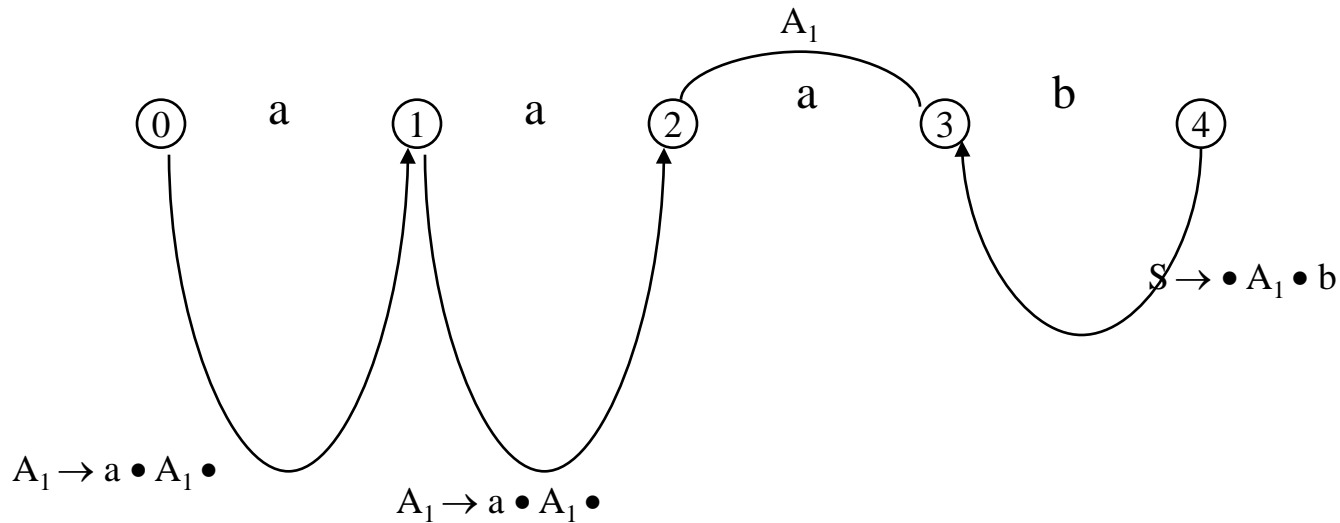
Parsing Chart Extensions ₅

Constraints in position 3



Parsing Chart Extensions ₆

propagation to positions 2 and 1



Parsing Chart Extensions ⁷

Head driven chart parsing

- Start rule application from the most informative/restrictive component
 - Linguistic motivation : HG, HPSG
 - Automatic acquisition
 - Generalization of left corner (LC) parsing
 - Generalización of left to write strategies
 - Extended Head Grammar

Parsing Chart Extensions ⁸

Island driven chart parsing

- Parsing starts BU from some dynamically determined positions of the input string (islands)
- How select them
 - Non ambiguous words
 - base NPs
 - Segments detected with high precision (speech)
- How to extend them
 - local approach
 - neighbouring approach

Tabular methods ₁

- Dynamic programming
- CFG
- CKI (Cocke, Kasami, Younger, 1967)
 - Grammar in CNF
- Earley 1969
- Extensible to unification, probabilistic, etc...

Tabular methods 2

$G = \langle N, \Sigma, P, S \rangle, G \in \text{CNF}, w = a_1 \dots a_n$

CKY

$\langle X, H, D \rangle$

$X = \{[A, i, j] \mid 0 \leq i < j \wedge A \in N_G\}$

$H = \{[A, j-1, j] \mid A \rightarrow a_j \in P_G \wedge 1 \leq j \leq n\}$

$D = \{[B, i, j], [C, j, k] \Rightarrow [A, i, k] \mid A \rightarrow BC \in P_G \wedge 0 \leq i < k < j\}$

$V(D) = \{[A, i, j] \mid A \Rightarrow^* a_{i+1} \dots a_j\}$

domain, set of items

set of de hypothesis

set of valid entities

set of deductive steps

Tabular methods ₃

CKY

spatial cost $O(n^2)$

temporal cost $O(n^3)$

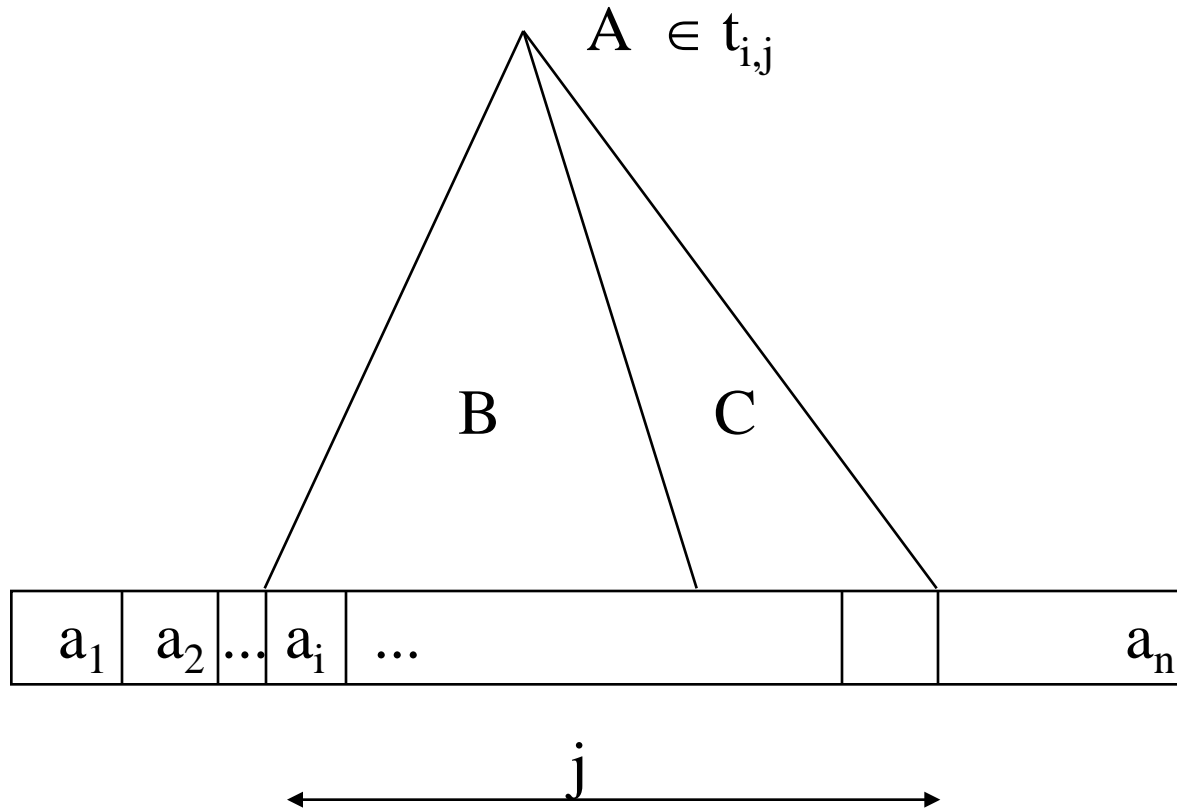
CNF

Dynamically build the parsing table

$$t_{ij} \quad 1 \leq i \leq |w|, 1 \leq j \leq |w| - i + 1$$

where $w = a_1, \dots, a_n$ is the input string

Tabular methods ₄



Where $A \rightarrow BC$ is a binary production of the grammar

Tabular methods ₅

That A is in cell t_{ij} means that from A the text fragment a_i, \dots, a_{i+j-1} (string of length j starting in i -esim position) can be derived.

The grammaticality condition is that the initial symbol of the grammar (F) satisfies $f \in t_{1|w|}$

Tabular methods ₆

The table is built BU

First row 1 is built using only the unary rules of the grammar:

row $j=1$

$$t_{i1} = \{A \mid [A \rightarrow a_i] \in P\}$$

Next rows $j=2, \dots$ are built. The key of the algorithm is that when row j is built all the previous ones (from 1 to $j-1$) are already built:

row $j > 1$

$$t_{ij} = \{A \mid \exists k, 1 \leq k < j, [A \rightarrow BC] \in P, B \in t_{ik}, C \in t_{i+k, j-k}\}$$

Tabular methods ⁷

1. Add the lexical edges
 2. for $w = 2$ to N :
 for $i = 0$ to $N-w$:
 for $k = 1$ to $w-1$:
 if:
 - $A \rightarrow BC$ *and*
 - $B \rightarrow \alpha \in \text{chart}[i, i+k]$ *and*
 - $C \rightarrow \beta \in \text{chart}[i+k, i+w]$
 then:
 - add $A \rightarrow BC$ to $\text{chart}[i, i+w]$
3. If $S \in \text{chart}[0, N]$, return the corresponding parse

taken from Loper

Tabular methods ₈

sentence → NP, VP

NP → A, B

VP → C, NP

A → det

B → n

NP → n

VP → vi

C → vt

Tabular methods ₉

| | | | |
|---|---|--------------------------------------|---------------------------------|
| <i>the cat eats fish</i> sentence | | | |
| <i>the cat eats</i> sentence | <i>cat eats fish</i> sentence | | |
| <i>the cat</i> NP | <i>cat eats</i> sentence | <i>eats fish</i> VP | |
| <i>the (det)</i> A | <i>cat (n)</i> B, NP | <i>eats (vt, vi)</i> C, VP | <i>fish (n)</i> B, NP |

Tabular methods 10

Earley

$$P_{\text{earley}} = \langle I, H, D \rangle$$

$$I = \{ [A \rightarrow \alpha \bullet \beta, i, j] \mid A \rightarrow \alpha \beta \in P_G \wedge 0 \leq i \leq j \}$$

$$D = D^{\text{init}} \cup D^{\text{scan}} \cup D^{\text{compl}} \cup D^{\text{pred}}$$

$$H = \{ [a_1, 0, 1], \dots, [a_n, n-1, n] \}$$

Initialization

$$D^{\text{init}} = \{ \Rightarrow [S \rightarrow \bullet \gamma, 0, 0] \}$$

$$D^{\text{scan}} = \{ [A \rightarrow \alpha \bullet a \beta, i, j], [a, j, j+1] \Rightarrow [A \rightarrow \alpha a \bullet \beta, i, j+1] \}$$

$$D^{\text{compl}} = \{ [A \rightarrow \alpha \bullet B \beta, i, j], [B \rightarrow \gamma \bullet, j, k] \Rightarrow [A \rightarrow \alpha B \bullet \beta, i, k] \}$$

$$D^{\text{pred}} = \{ [A \rightarrow \alpha \bullet B \beta, i, j] \Rightarrow [B \rightarrow \bullet \gamma, j, j] \}$$

scanning

completion

prediction

$$V = \{ [A \rightarrow \alpha \bullet \beta, i, j] \mid \alpha \Rightarrow^* a_{i+1} \dots a_j \wedge S \Rightarrow^* a_1 \dots a_i A \gamma \}$$

$$F = \{ [S \rightarrow \gamma \bullet, 0, n] \}$$

$$C = \{ [S \rightarrow \gamma \bullet, 0, n] \mid \gamma \Rightarrow^* a_1 \dots a_n \}$$

Tabular methods ₁₁

spatial cost $O(n^2)$

temporal cost $O(n^3)$, $O(n^2)$ for non ambiguous grammars

CNF not needed

TD strategy

| | | |
|----|---|-----------|
| S | → | NP, VP. |
| NP | → | *N. |
| NP | → | *DET, *N. |
| VP | → | *V, NP. |

Tabular methods ¹²

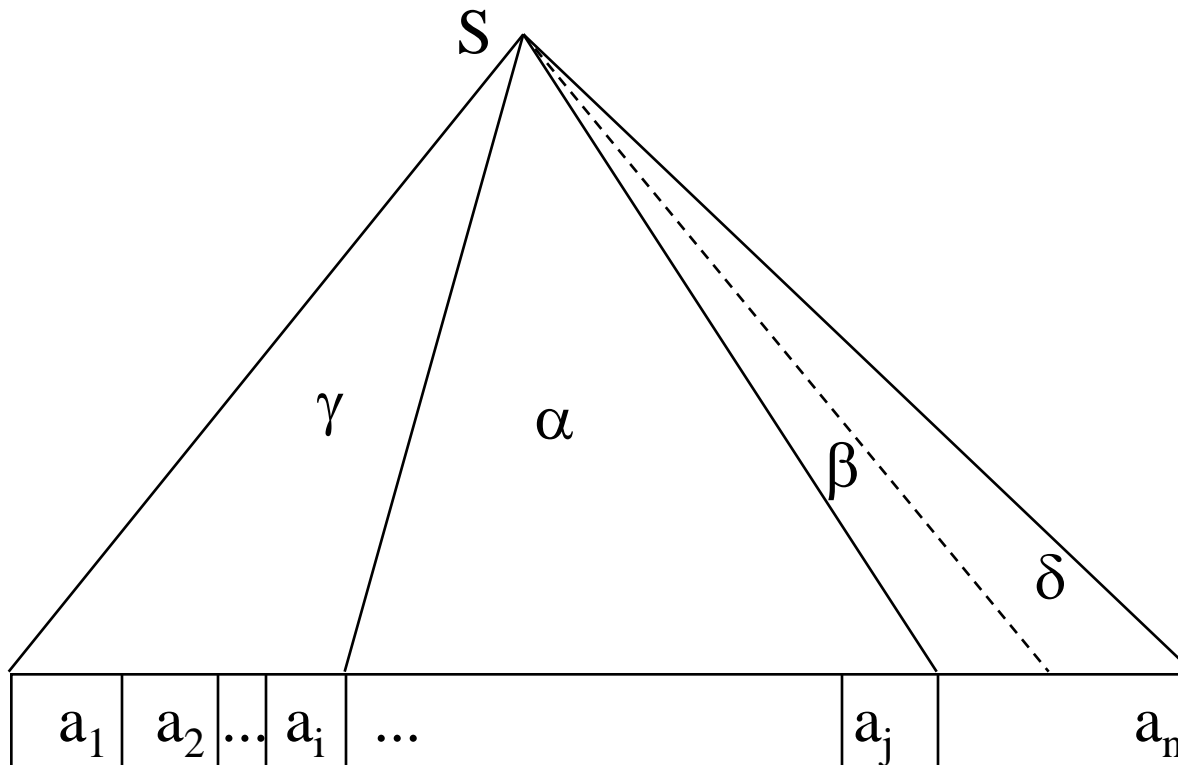
Each state corresponds to consuming one word from the input string: $I_0, I_1, \dots, I_i, \dots, I_{|w|}$

Each state contains sets of “parse list” indicating the process of application of a rule (as a dotted rule) for reaching the state

$[A \dashrightarrow \alpha \bullet \beta, i] \in I_j$ means that $S \dashrightarrow \gamma A \delta$ where
 $\gamma \dashrightarrow a_1 a_2 \dots a_i$ $\alpha \dashrightarrow a_{i+1} a_{i+2} \dots a_j$

Gramaticality condition is $[S \dashrightarrow \alpha \bullet, 0] \in I_{|w|}$

Tabular methods ¹³



$$S \dashrightarrow \gamma A \delta$$

$$[A \dashrightarrow \alpha \bullet \beta, i] \in I_j$$

Iterative process:

Building I_0

Building (extension) the rest of states

operations:

TD prediction

scanning

completion (end of a rule)

Building I_0 :

- 1) if $[S \rightarrow \alpha] \in P$ then $[S \rightarrow \bullet \alpha, 0] \in I_0$
- 2) if $[B \rightarrow \gamma \bullet, 0] \in I_0$
(only possible if $[B \rightarrow \bullet, 0] \in I_0$)
and $[A \rightarrow \alpha \bullet B \beta, 0] \in I_0$ then $[A \rightarrow \alpha B \bullet \beta, 0] \in I_0$
- 3) if $[A \rightarrow \alpha \bullet B \beta, 0] \in I_0$ and $[B \rightarrow \gamma] \in P$
then $[B \rightarrow \bullet \gamma, 0] \in I_0$

Extension:

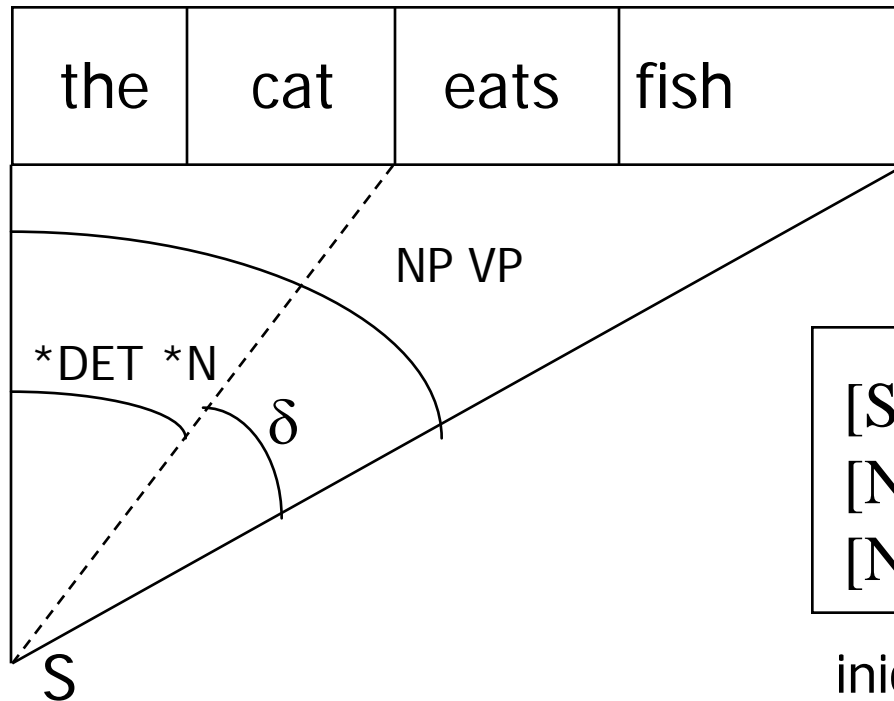
4) if $[B \rightarrow \alpha \bullet a\beta, i] \in I_{j-1}$ and $a = a_j$ then $[B \rightarrow \alpha a \bullet \beta, i] \in I_j$
(scanning)

5) if $[A \rightarrow \gamma \bullet, i] \in I_j$ and $[B \rightarrow \alpha \bullet A\beta, k] \in I_i$ then
 $[B \rightarrow \alpha A \bullet \beta, k] \in I_j$
(completion)

6) if $[A \rightarrow \alpha \bullet B\beta, i] \in I_j$ and $[B \rightarrow \gamma] \in P$
then $[B \rightarrow \bullet \gamma, j] \in I_j$
(prediction)

Tabular methods ¹⁷

example:



$[S \rightarrow \bullet NP VP, 0] \in I_0$

$[NP \rightarrow \bullet *N, 0] \in I_0$

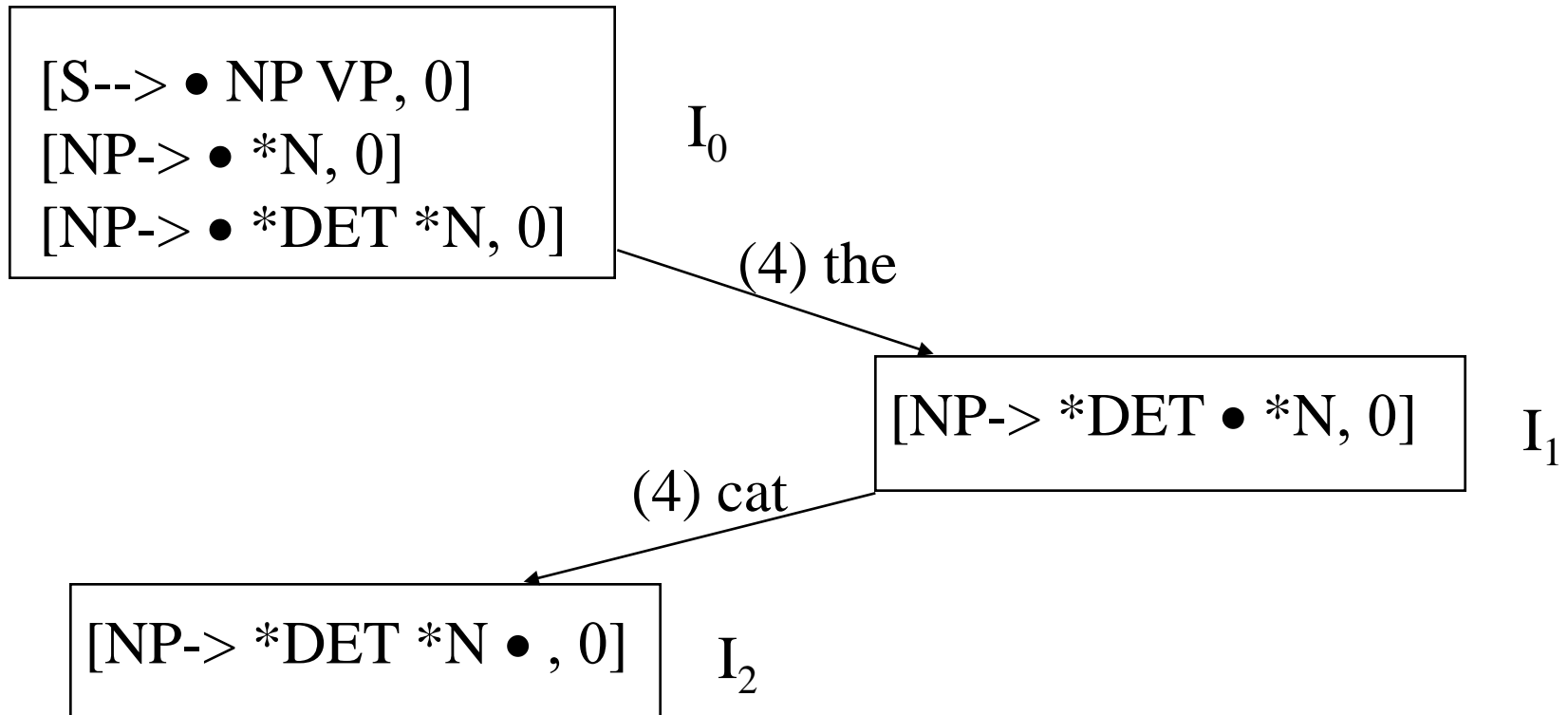
$[NP \rightarrow \bullet *DET *N, 0] \in I_0$

inicialization

prediction

prediction

Tabular methods ¹⁸



Tabular methods ₁₉

